

COMPUTATIONAL PROTEOMICS AND METABOLOMICS

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5. Quantification II: Label-free quantification, SILAC



Overview

- Label-free quantification
 - Definition of features
 - Feature finding on centroided data
 - Absolute quantification using label-free quantification
- SILAC quantification
 - Problem
 - Application of simple feature finding and linking
 - MaxQuant algorithm
 - Application examples

LEARNING UNIT 5A

FEATURE FINDING FOR

LABEL-FREE QUANTIFICATION

Feature-finding

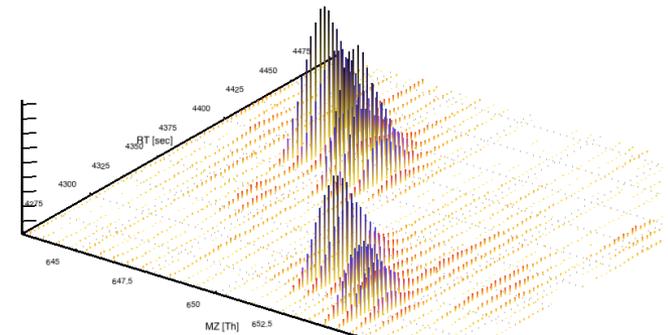
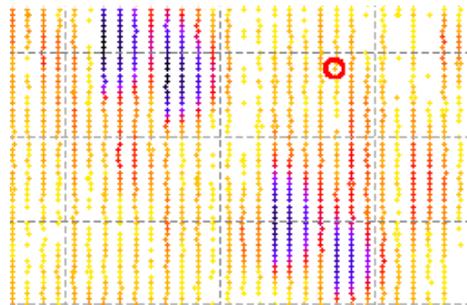
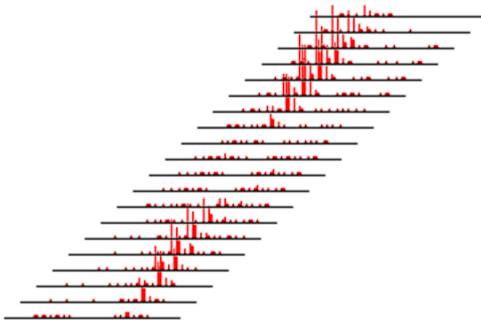
- Definition of terms (maps, features)
- Key concepts in label-free quantification
- Average model
- Feature finding on centroided data

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Label-Free Quantification (LFQ)

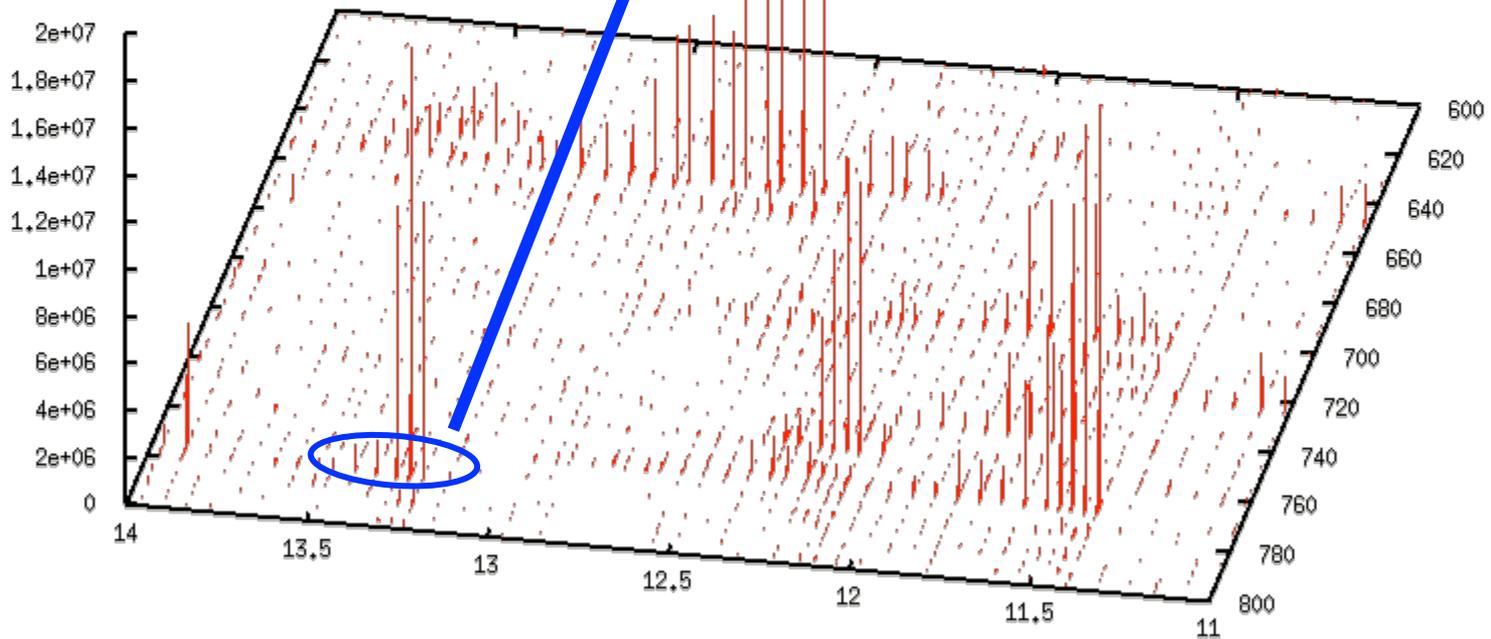
- **Quantification through the ion current in MS spectra**
- Key advantage: no labeling needed – cheap, scales well
- Key disadvantage: normalization tricky – direct comparison
- Based on the notion of **features** and **maps**
 - LC-MS data: 2D datasets of up to hundreds of GB per sample
 - **Raw data**: unmodified detector signal
 - **Centroided data**: peaks called on the MS level
 - **Features**: the stuff that matters in **maps**



LC-MS Data (Map)

Quantification

(15 nmol/ μ l, 3x over-expressed, ...)



Feature Finding – Terms

Map:

Two-dimensional data set (RT, m/z) containing the MS signal from one LC-MS run.

Feature:

The sum of all the MS signals caused by the same analyte in a specific charge state.

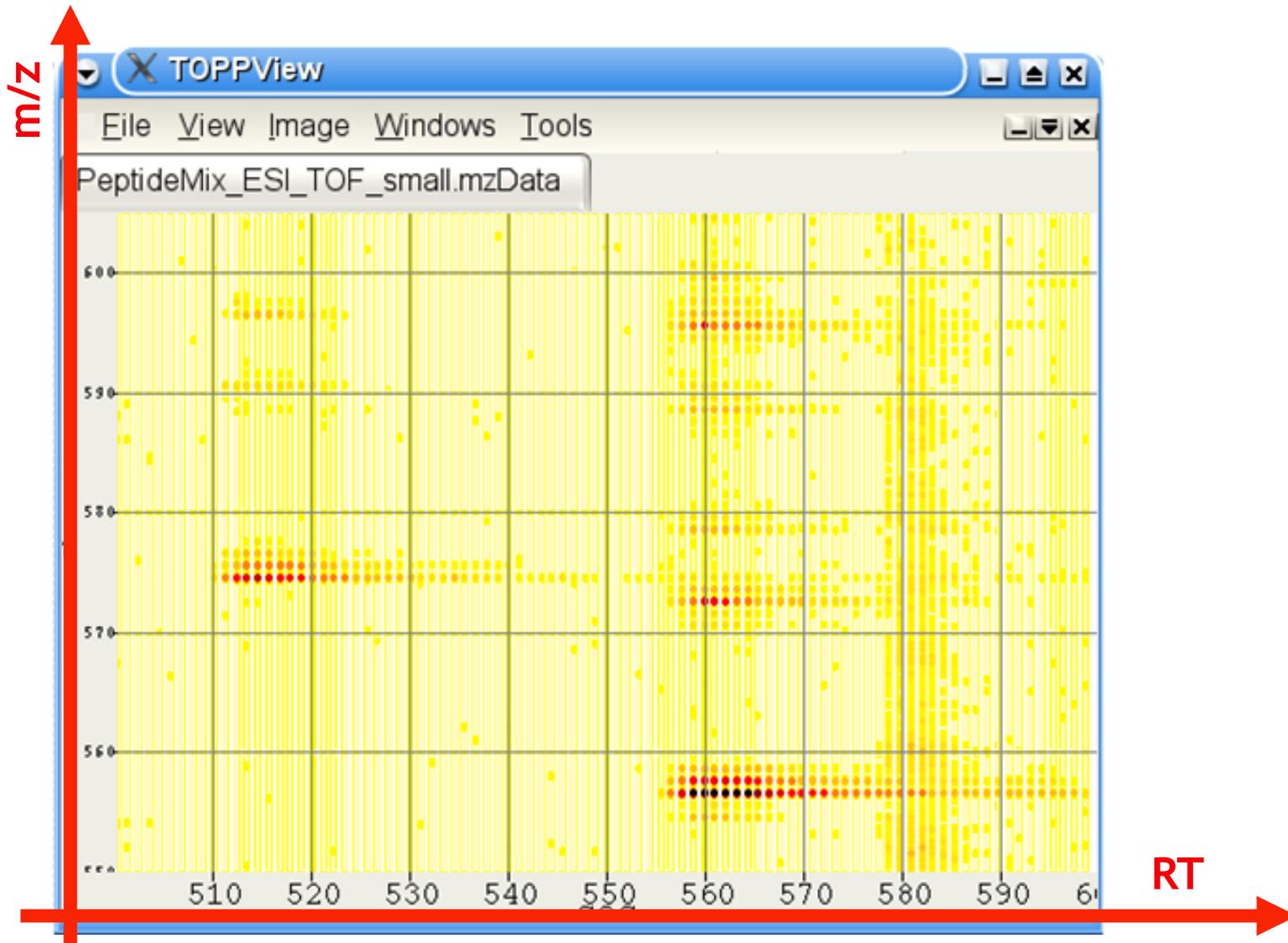
Different charge states or adducts will result in distinct features. Primarily characterized by RT, m/z, charge, intensity.

Feature finding:

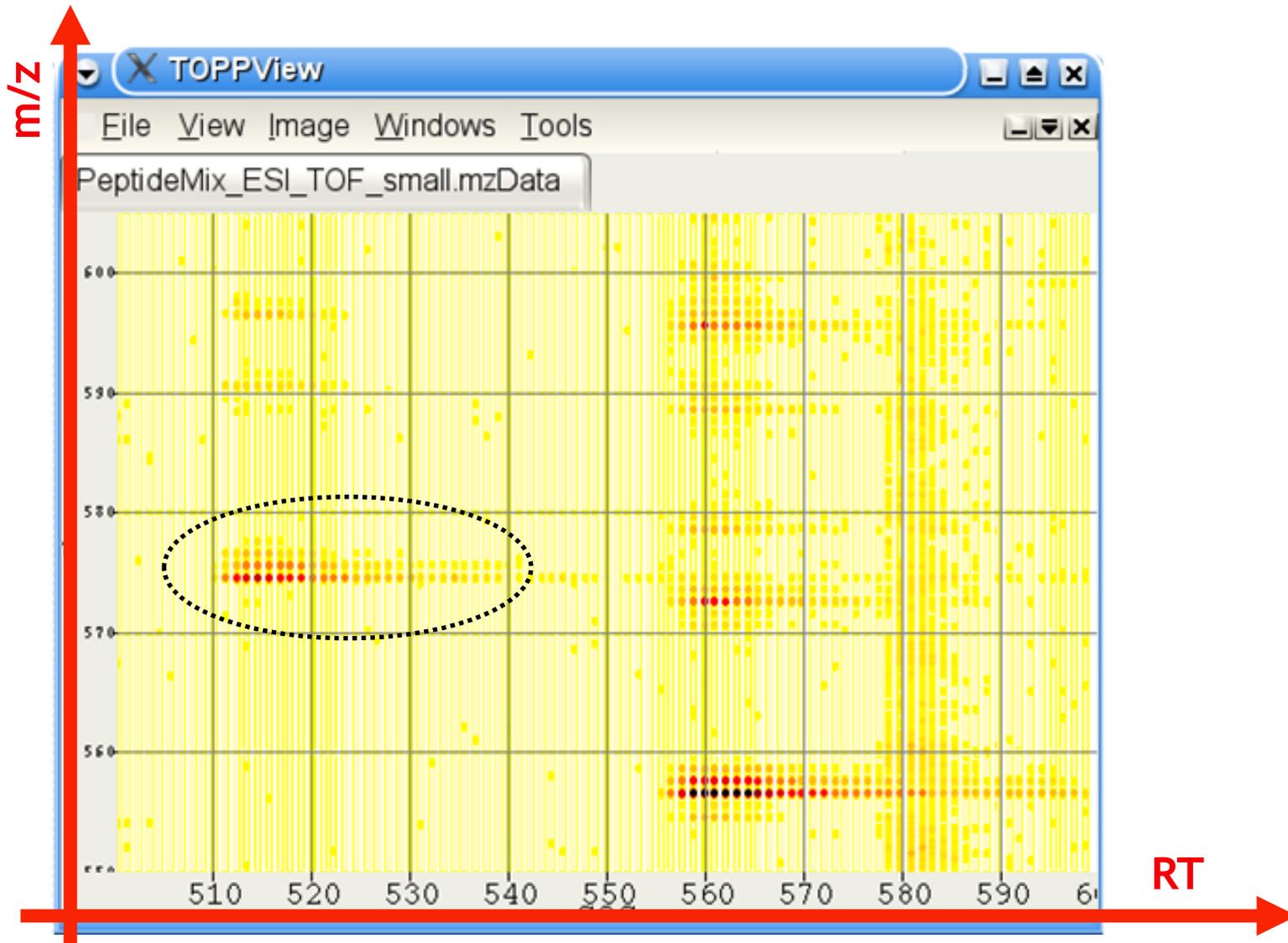
Finding the set of features explaining as much of the signal in a map as possible.



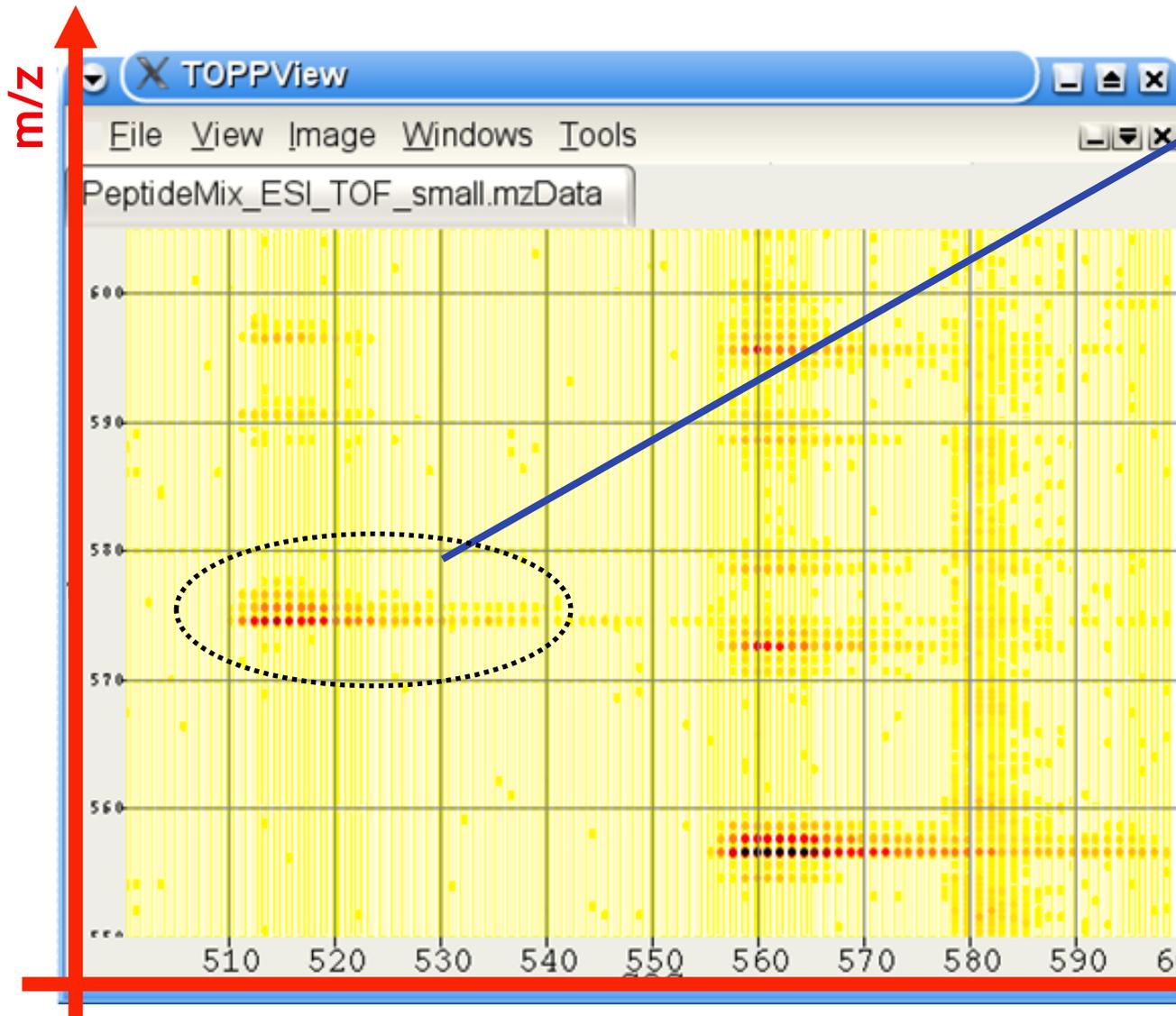
Raw Map



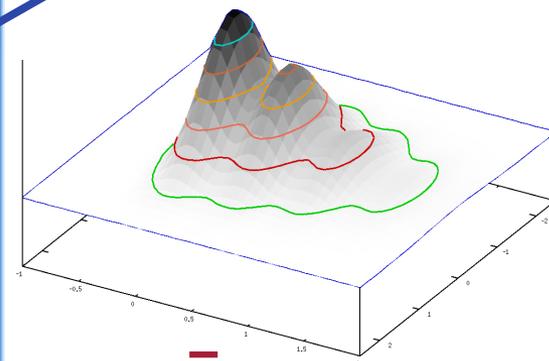
Raw Map



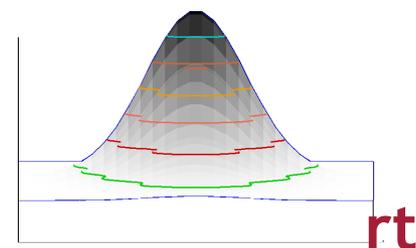
Raw Map



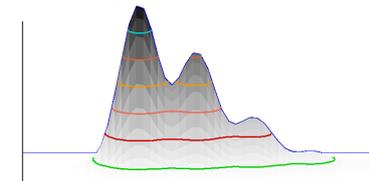
Feature



=



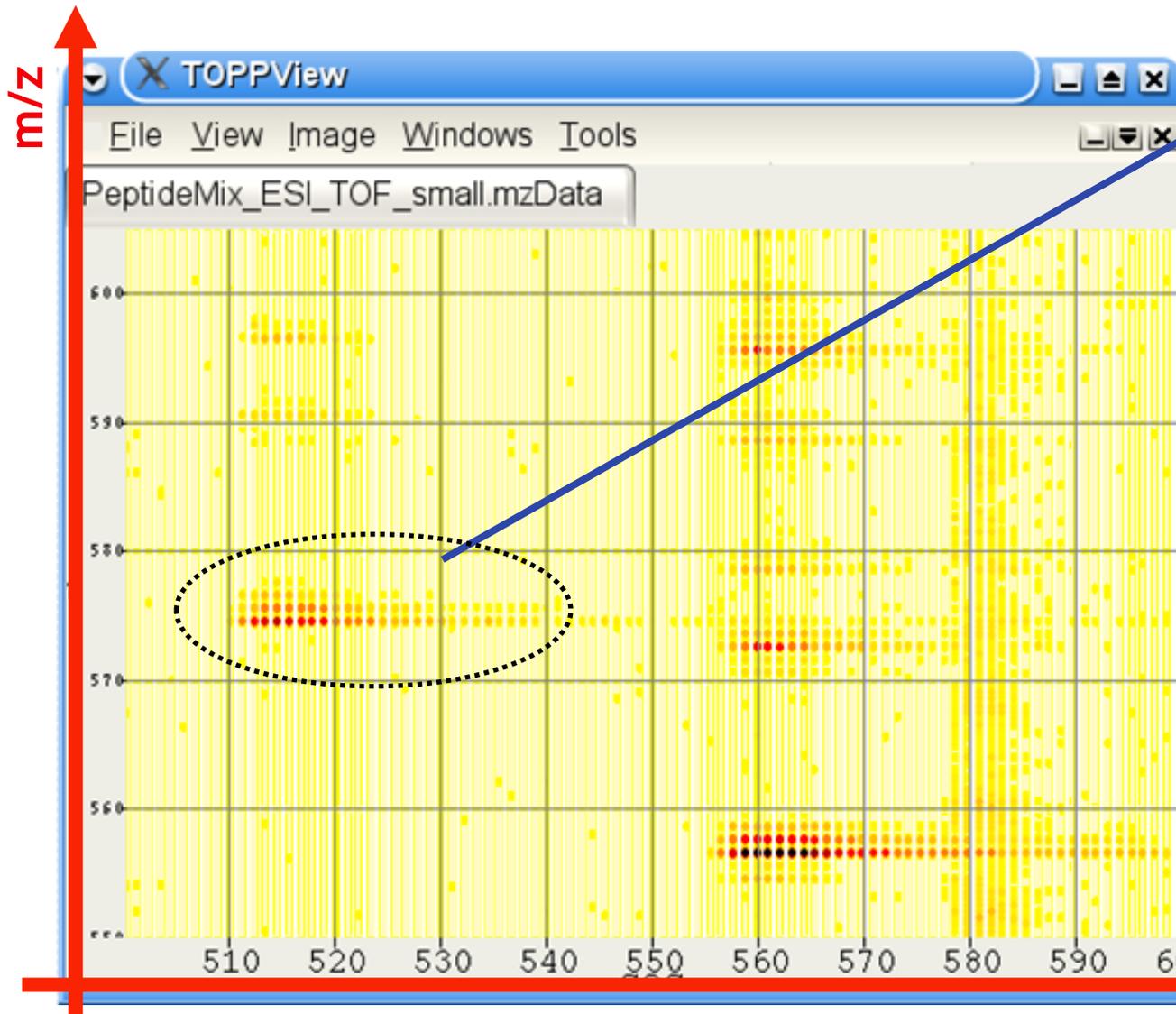
+



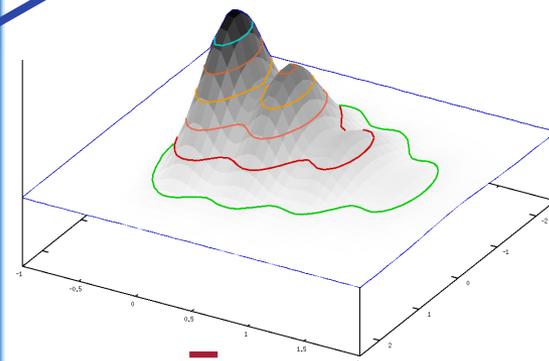
RT

m/z

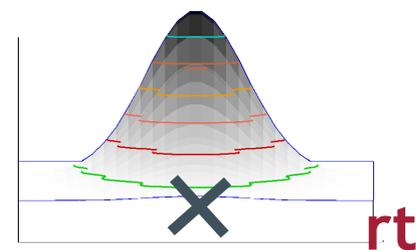
Raw Map



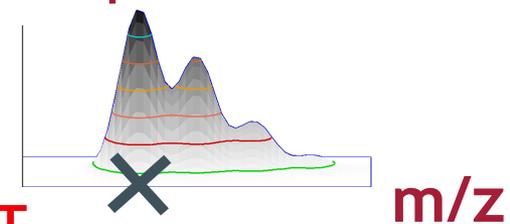
Feature



=



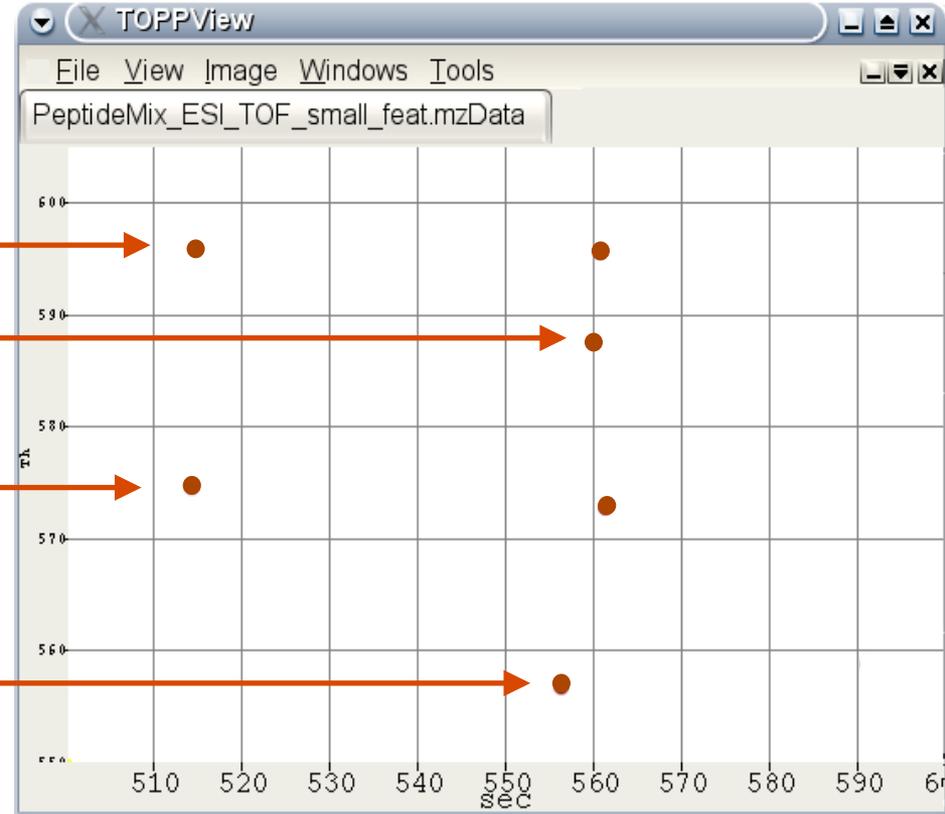
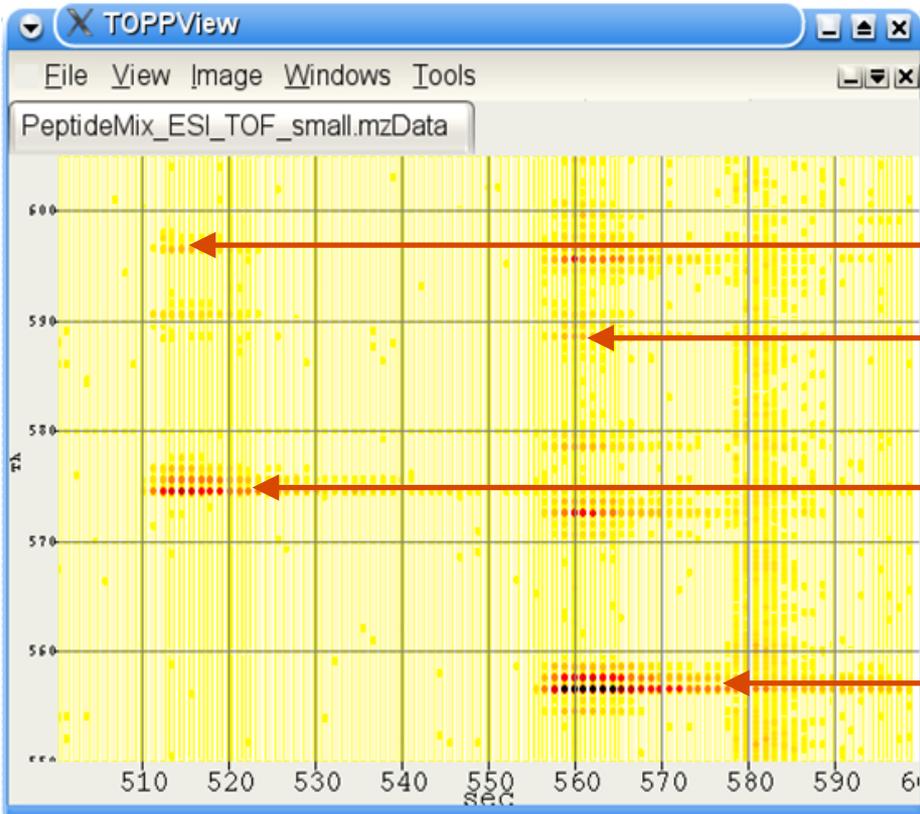
+



RT

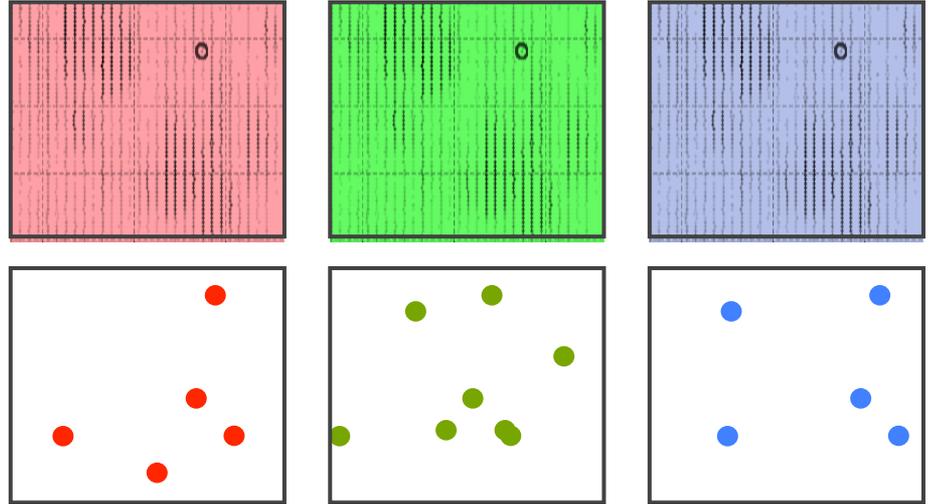
m/z

Raw Map → Feature Map



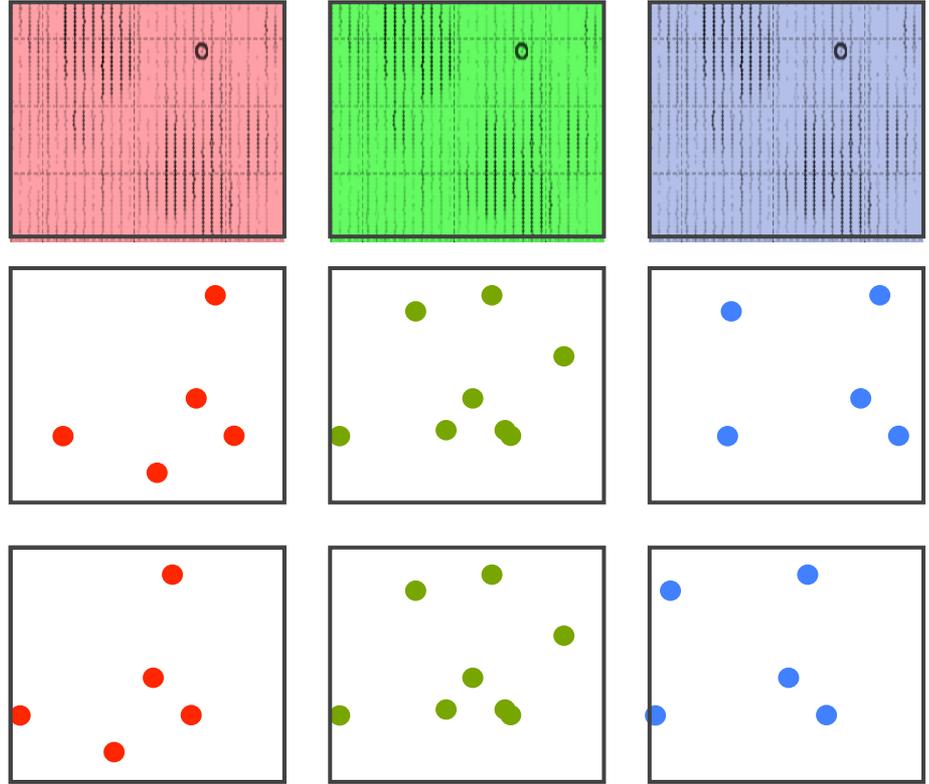
LFQ – Analysis Strategy

1. **Find** features in all maps



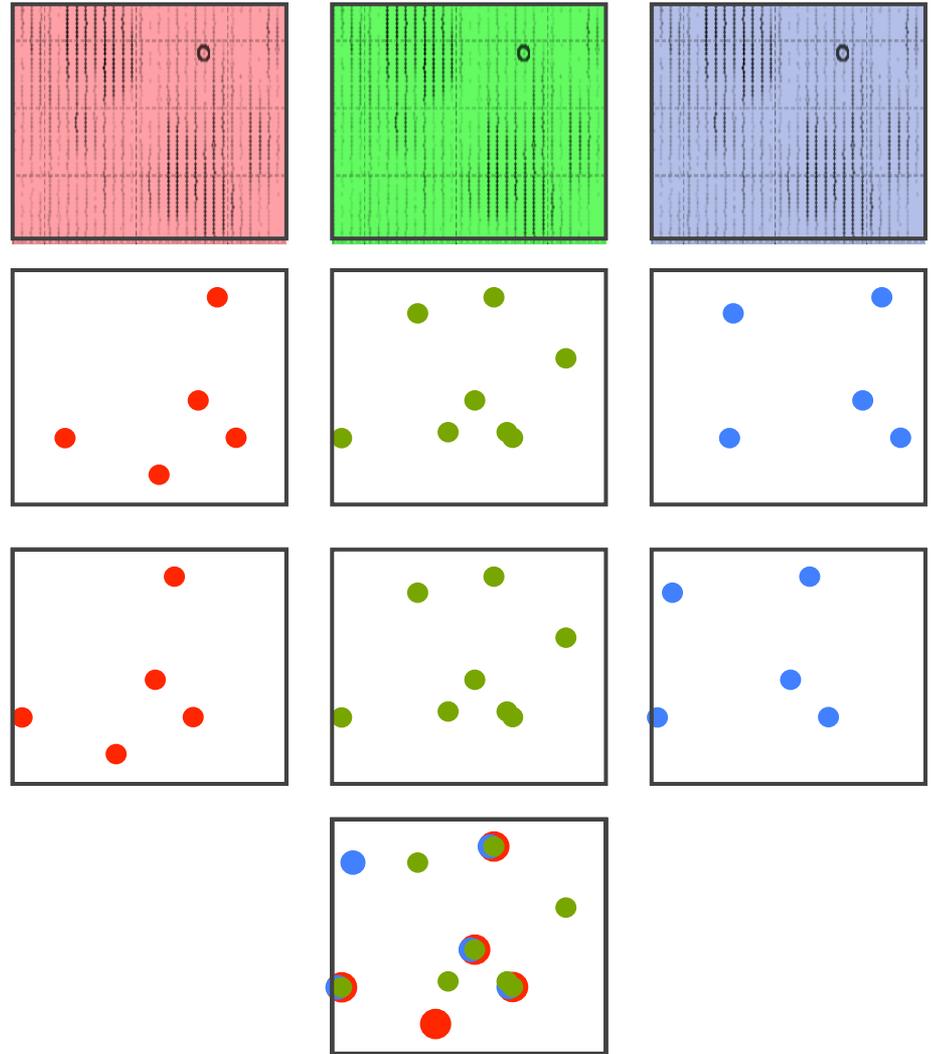
LFQ – Analysis Strategy

1. **Find** features in all maps
2. **Align** maps



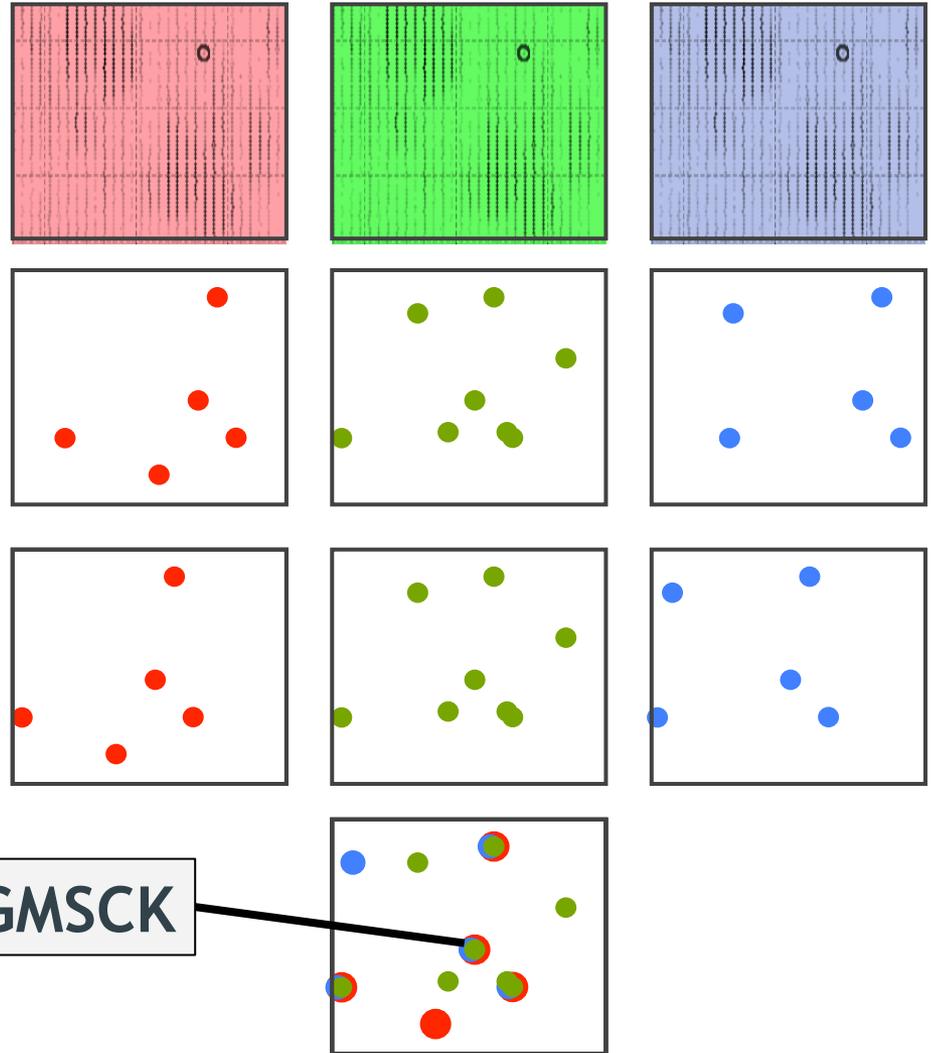
LFQ – Analysis Strategy

1. **Find** features in all maps
2. **Align** maps
3. **Link** corresponding features



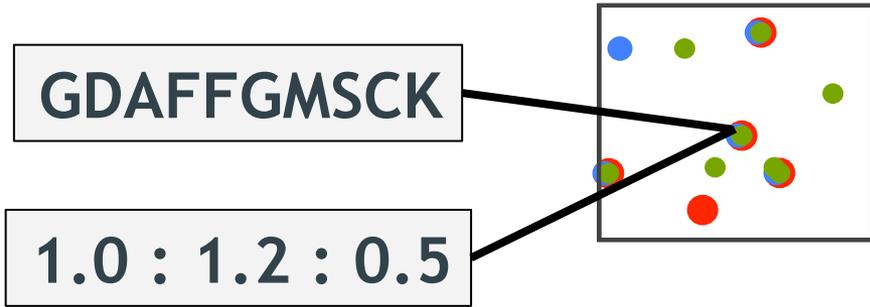
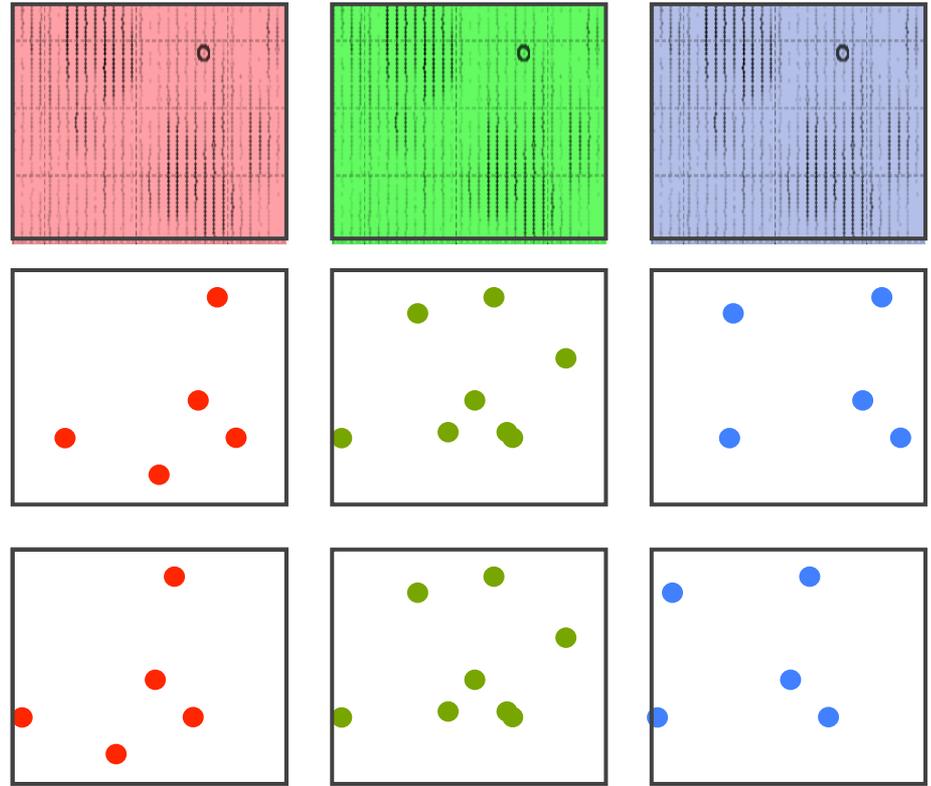
LFQ – Analysis Strategy

1. **Find** features in all maps
2. **Align** maps
3. **Link** corresponding features
4. **Identify** features

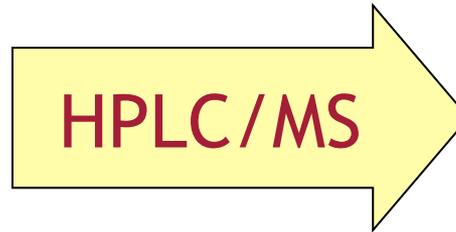


LFQ – Analysis Strategy

1. **Find** features in all maps
2. **Align** maps
3. **Link** corresponding features
4. **Identify** features
5. **Quantify**



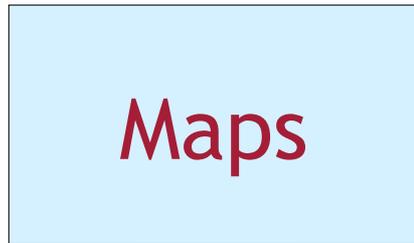
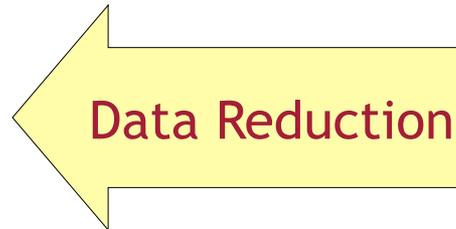
Feature Finding as Data Reduction



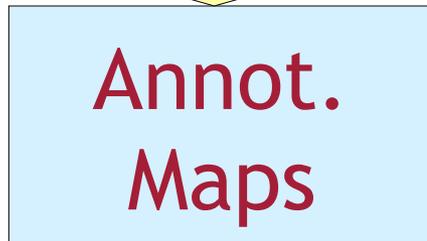
10 GB



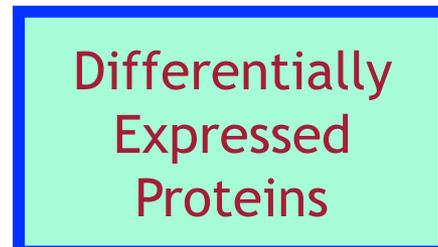
1 GB



50 MB



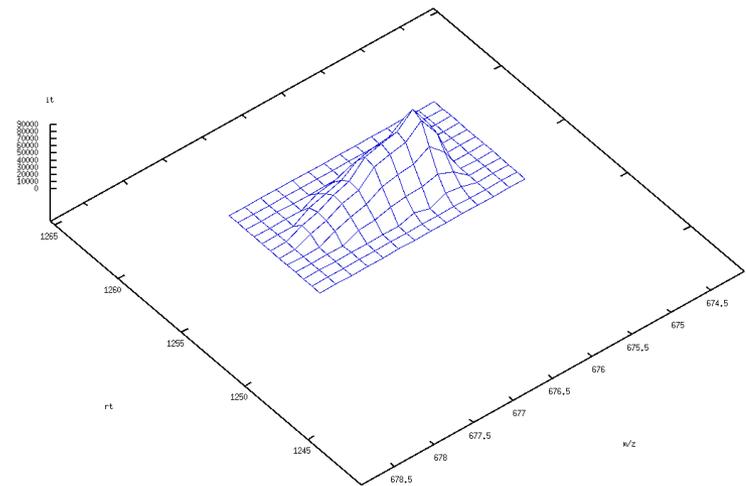
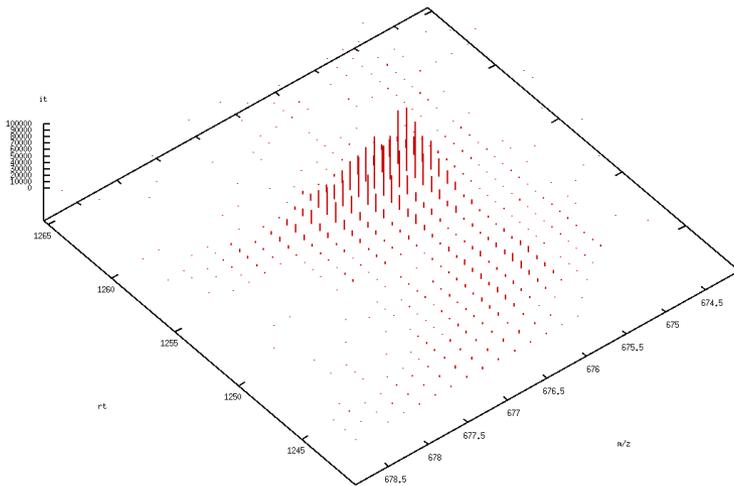
50 MB



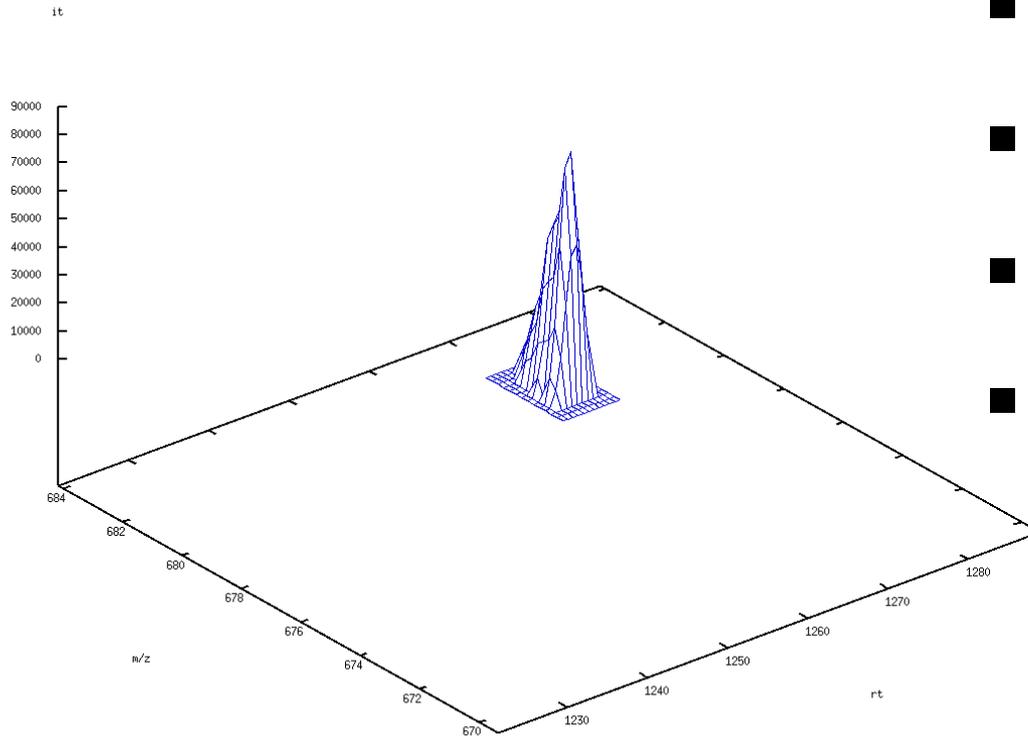
1 kB

Feature Finding

- Identify all peaks belonging to one peptide
- Key idea:
 - Identify suspicious regions
 - Fit a two-dimensional model to that region



Feature Attributes

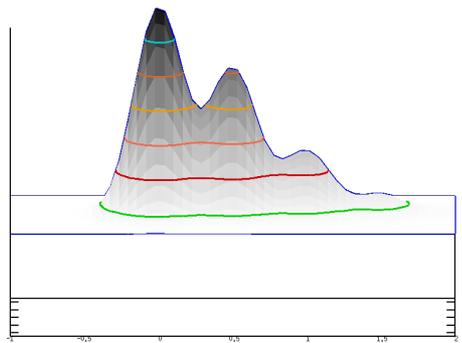
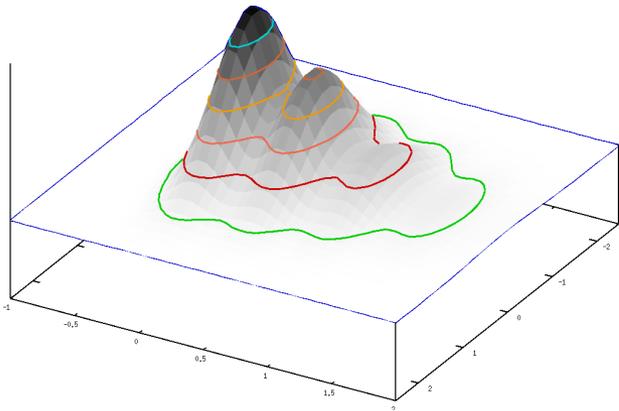


Attributes

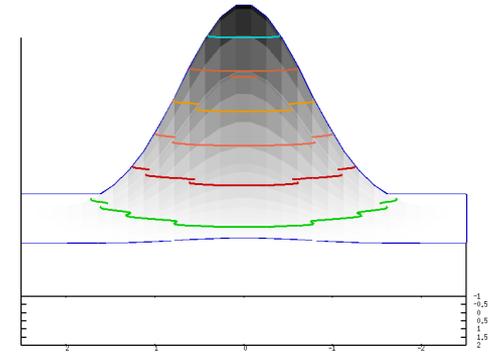
- Position (m/z , RT)
- Intensity, **volume**
- Quality
-

Feature Model

Feature model = Isotope pattern x Elution profile



m/z



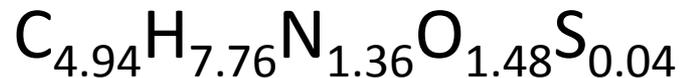
rt

Feature Model

- Physical processes leading to the shape of a feature:
 - Chromatography
 - Elution profiles are (ideally) shaped like a Gaussian
 - Parameters: width, height, position
 - Mass spectrometry
 - Mass spectra of peptides are characterized by the isotope pattern
 - Modeled by a binomial distribution
- Both **separation processes are independent**
- A two-dimensional feature is then described by the product of two one-dimensional models

Averagine

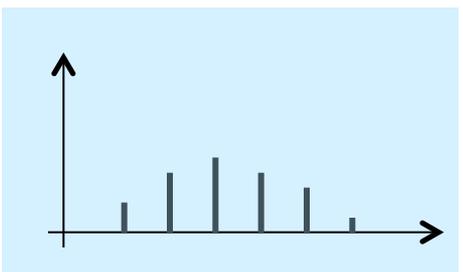
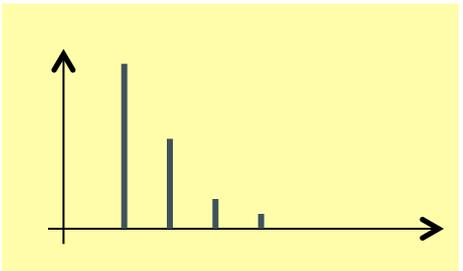
- Since the isotope pattern changes with the composition of the peptide, it is unknown which pattern should be fitted!
- Idea
 - We know the mass of the feature
 - Assume an average composition of an amino acid
 - Then we can estimate the composition
- The elemental composition of such an average amino acid, also called 'averagine', can be derived statistically:



Isotope Patterns

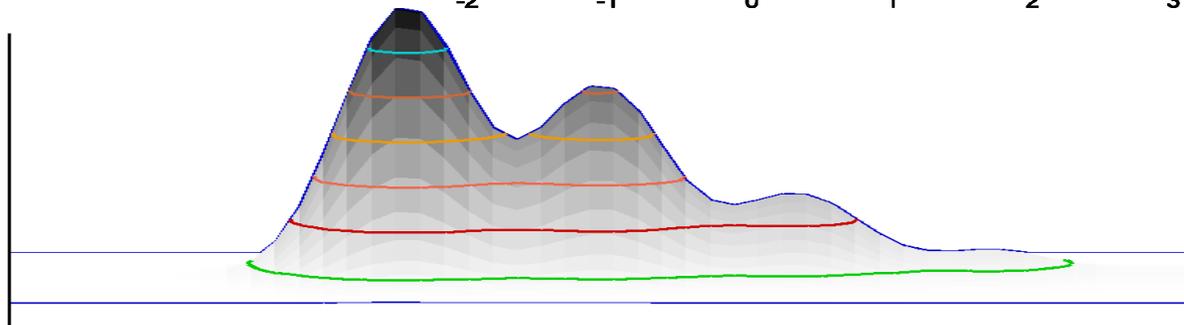
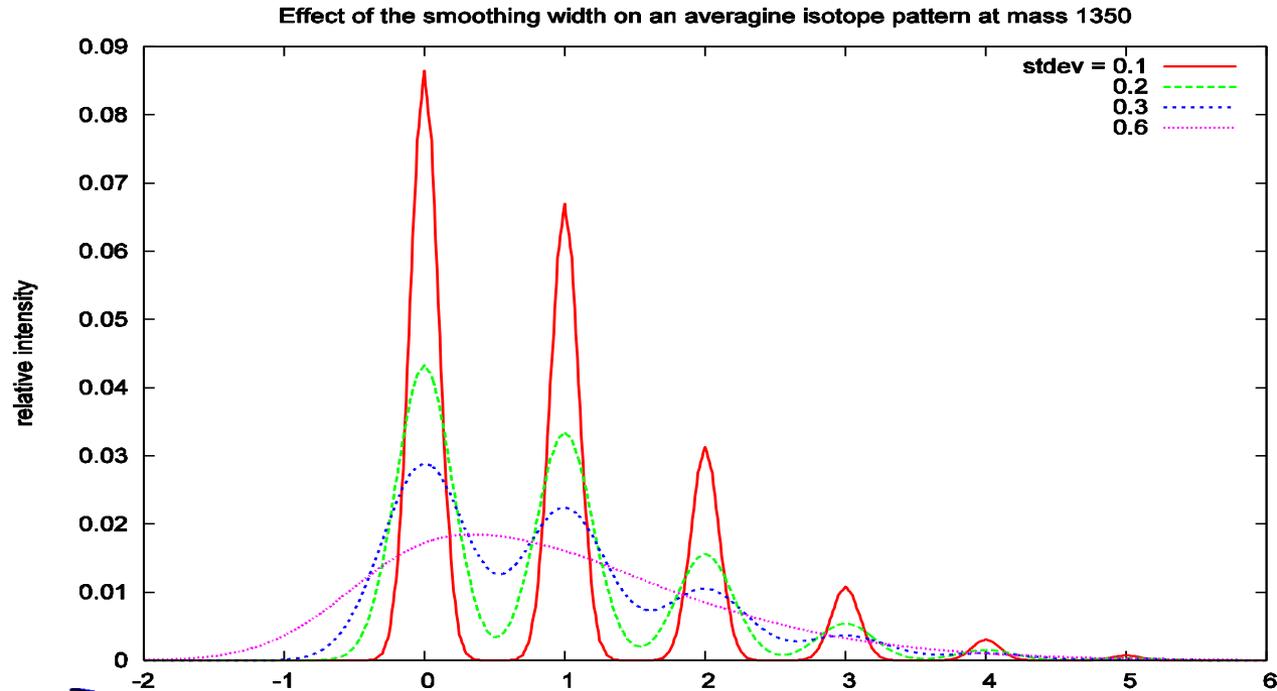
- Based on average compositions one can compute the isotope patterns for any given m/z
- Heavier peptides have smaller monoisotopic peaks
- In the limit, the distribution approaches a normal distribution

m [Da]	P ($k=0$)	P ($k=1$)	P ($k=2$)	P ($k=3$)	P ($k=4$)
1000	0.55	0.30	0.10	0.02	0.00
2000	0.30	0.33	0.21	0.09	0.03
3000	0.17	0.28	0.25	0.15	0.08
4000	0.09	0.20	0.24	0.19	0.12



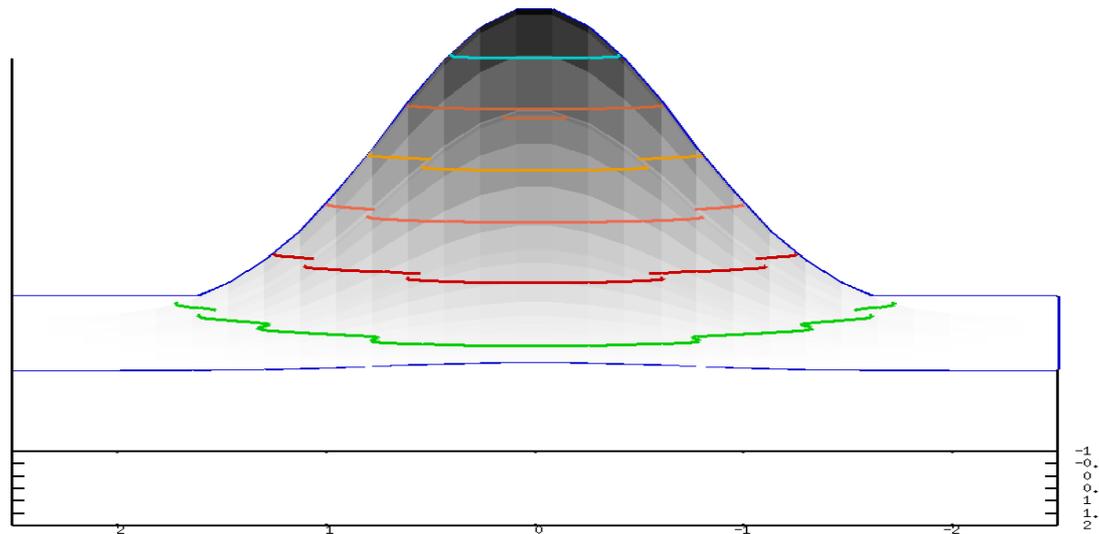
Feature Model – m/z

- Isotope pattern is also modulated by the **instrument resolution**
- We can assume a Gaussian shape for each of the peaks of the isotope pattern



Feature Model – RT

- Elution profile is typically assumed to be a Gaussian
- There are some variants that also allow for asymmetric peaks
- This defines the shape of a feature in in the RT dimension



Feature Finding – Algorithm

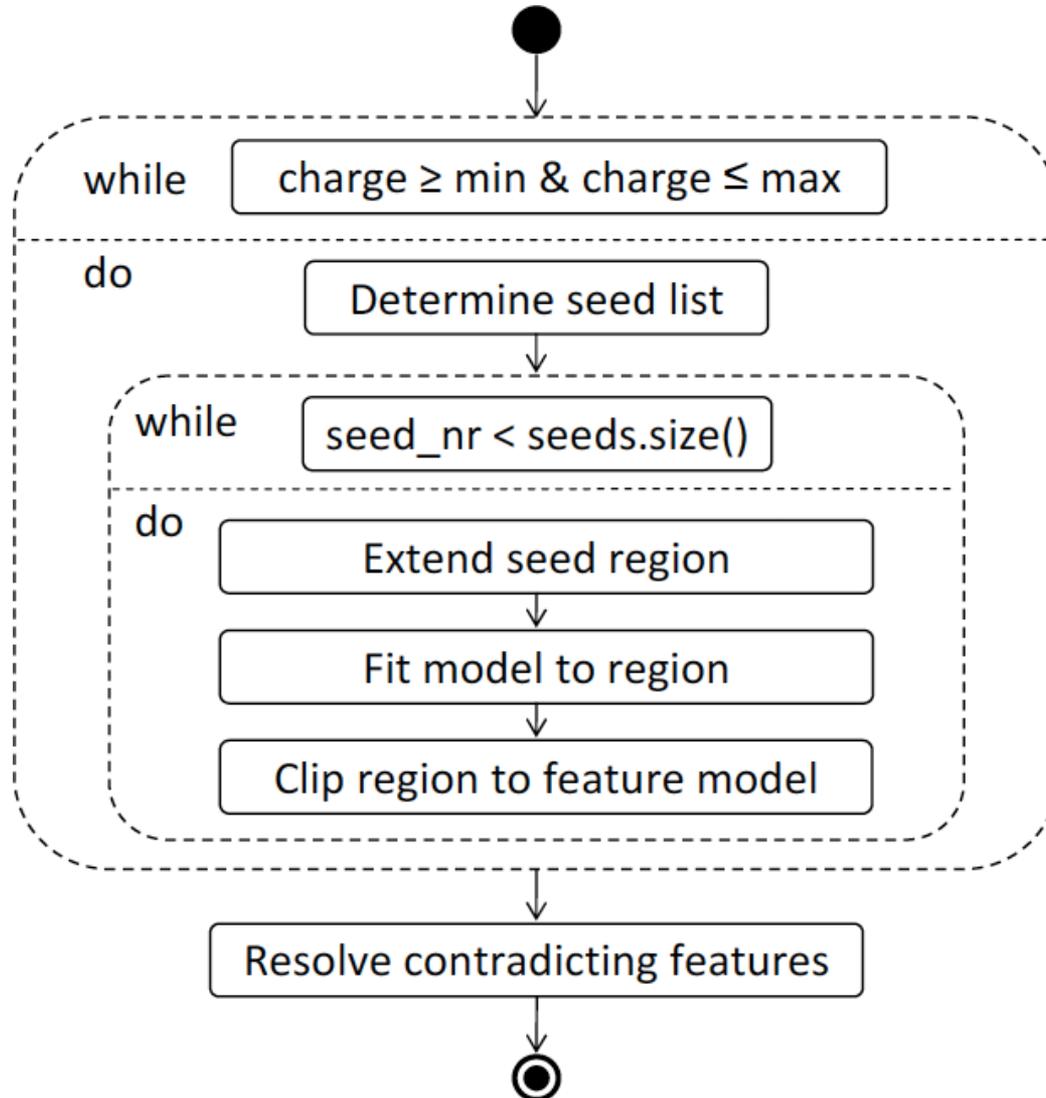
Most algorithms consists of four phases

- 1. Seeding.** *Choose peaks of high intensities, as those are usually in features (“seeds”).*
- 2. Extension.** *Conservatively add peaks around the seed, never mind if you pick up a few peaks too many.*
- 3. Modeling.** *Estimate parameters of a two-dimensional feature for the region.*
- 4. Refinement.** *Optimally fit a model to the collected peaks. Remove peaks not agreeing with the model. Iterate until convergence.*

Algorithm: Seeding

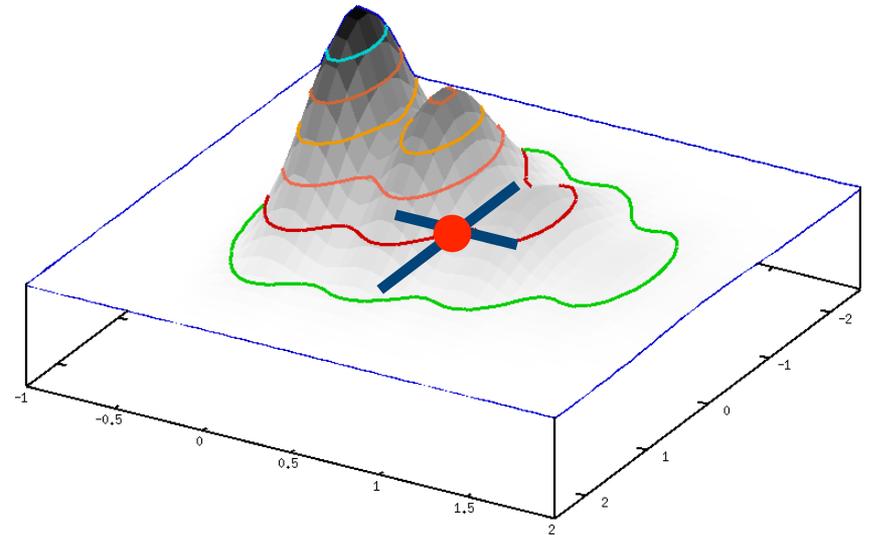
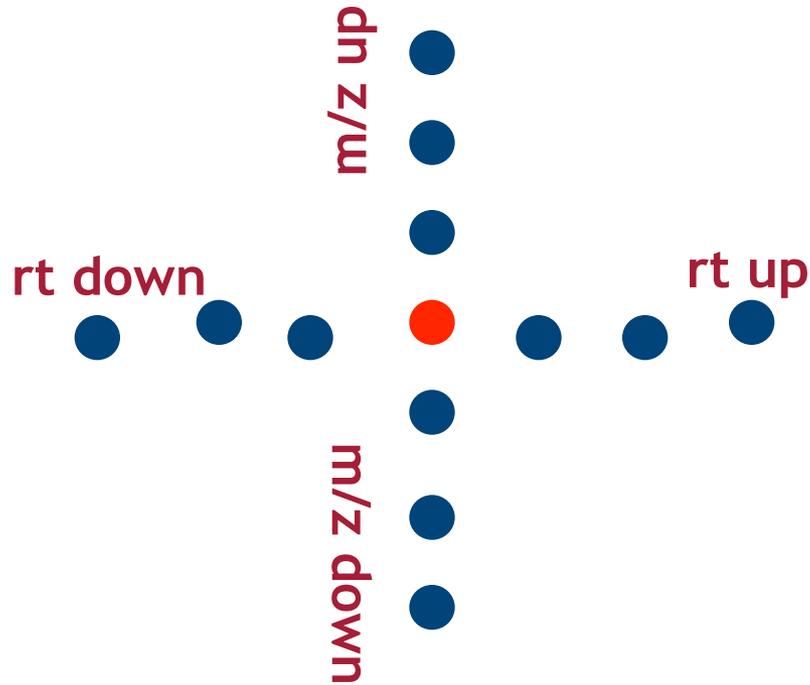
- Start with the highest peaks in the map
- Pick only one seed per feature, thus exclude peaks of already identified features for later seeding
- More advanced variants of the algorithm use Wavelet techniques to detect the best seeds
- **Problems**
 - Low-intensity features have intensities barely above the surrounding noise
 - Choose a threshold based on the average noise
 - Dilemma:
 - threshold too high, features will not get seeded
 - Threshold too low, millions of noise peaks will be considered as seeds
HUGE run times

Feature Finding – Overview



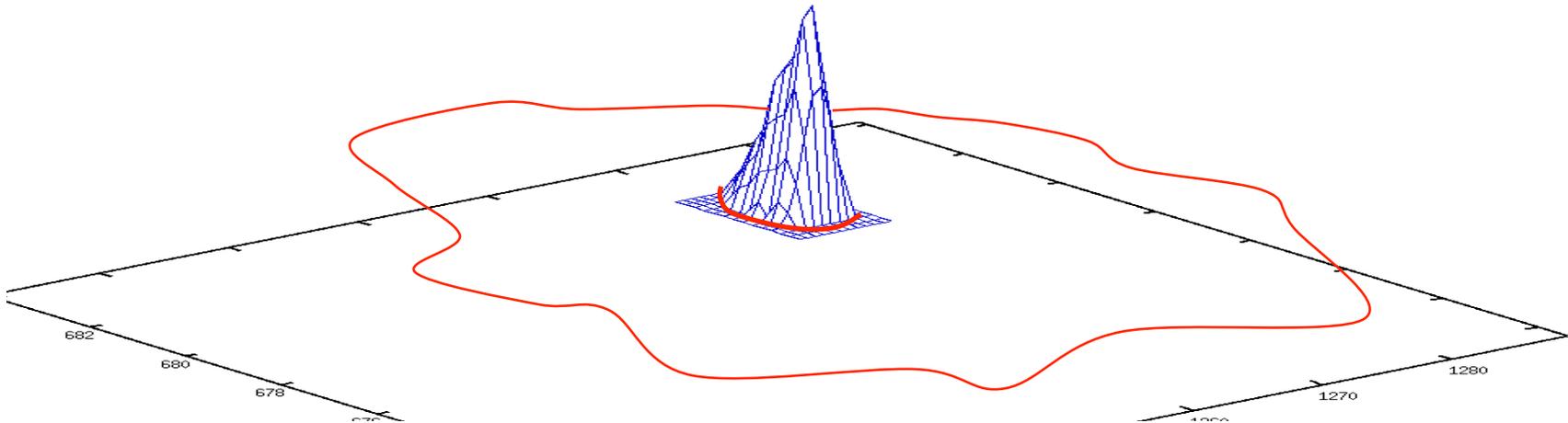
Algorithm: Extension

- Explore the peaks around the seed
- Add them to a set of relevant peaks
- Abort if the peaks are getting too small or too far away



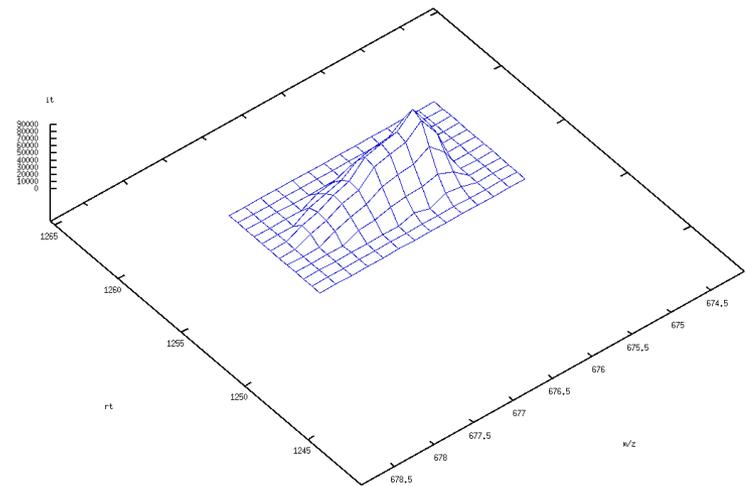
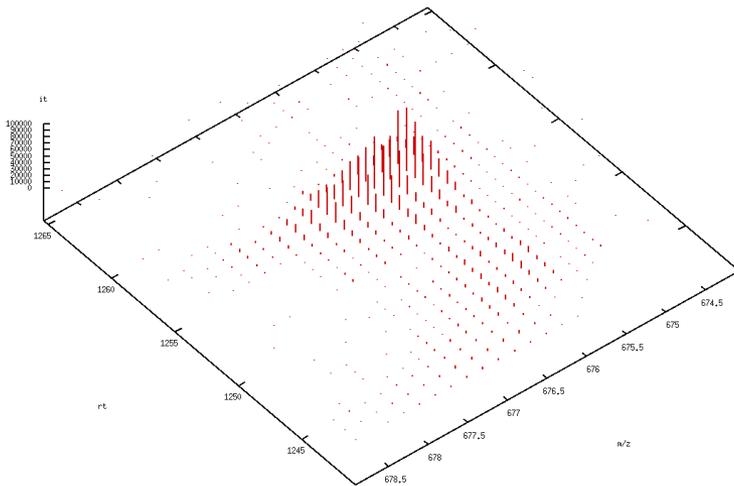
Algorithm: Refinement

- **Remove peaks** that are not consistent with the model
- **Determine optimal model** for the reduced set of peaks
- Iterate this until no further improvement can be achieved
- Remove all peaks of this feature from potential seeds



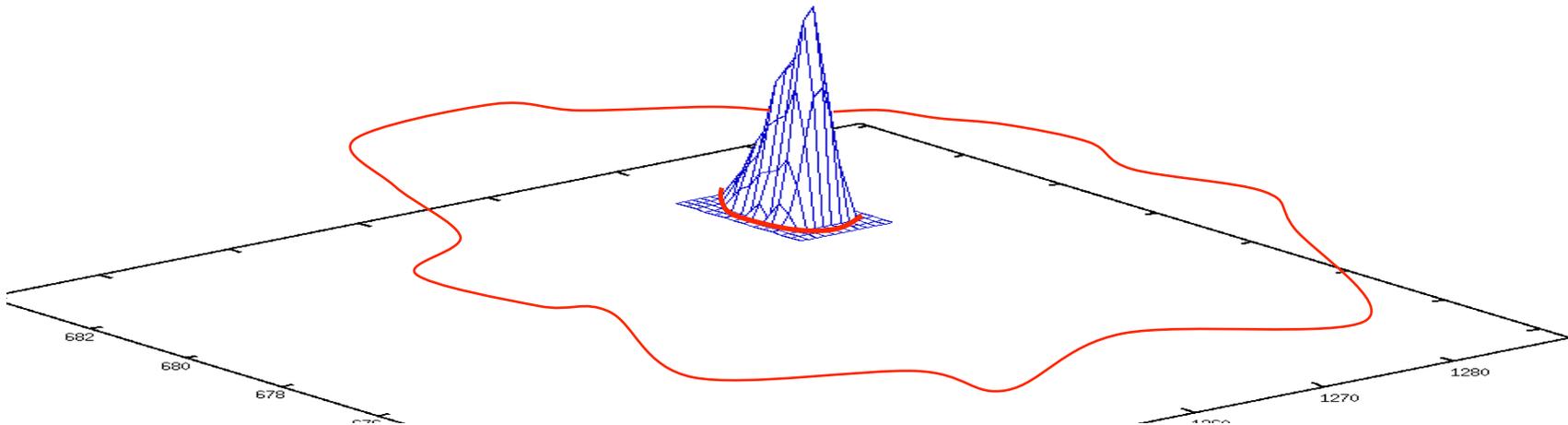
Feature Finding

- Identify all peaks belonging to one peptide
- Key idea:
 - identify suspicious regions
 - Fit a **model** to that region and identify peaks are explained by it



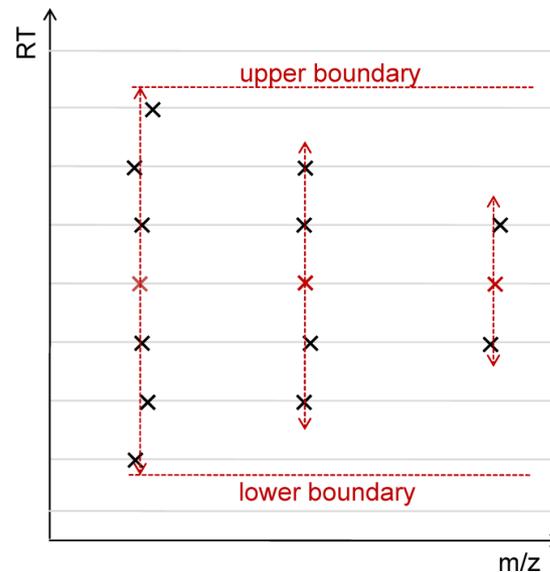
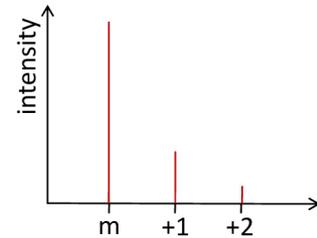
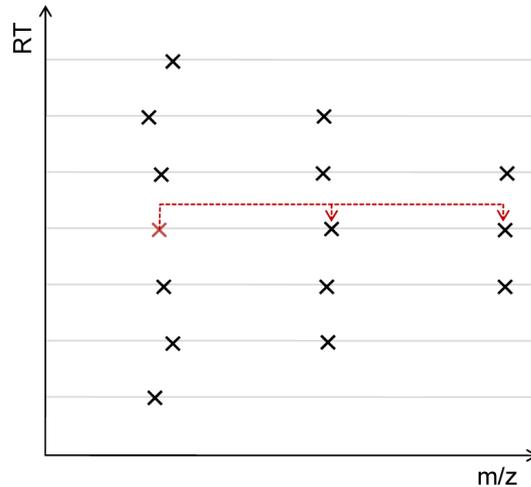
Feature Finding

- **Extension:** collect all data points close to the seed
- **Refinement:** remove peaks that are not consistent with the model
- **Fit an optimal model** for the reduced set of peaks
- Iterate this until no further improvement can be achieved



Collecting Mass Traces

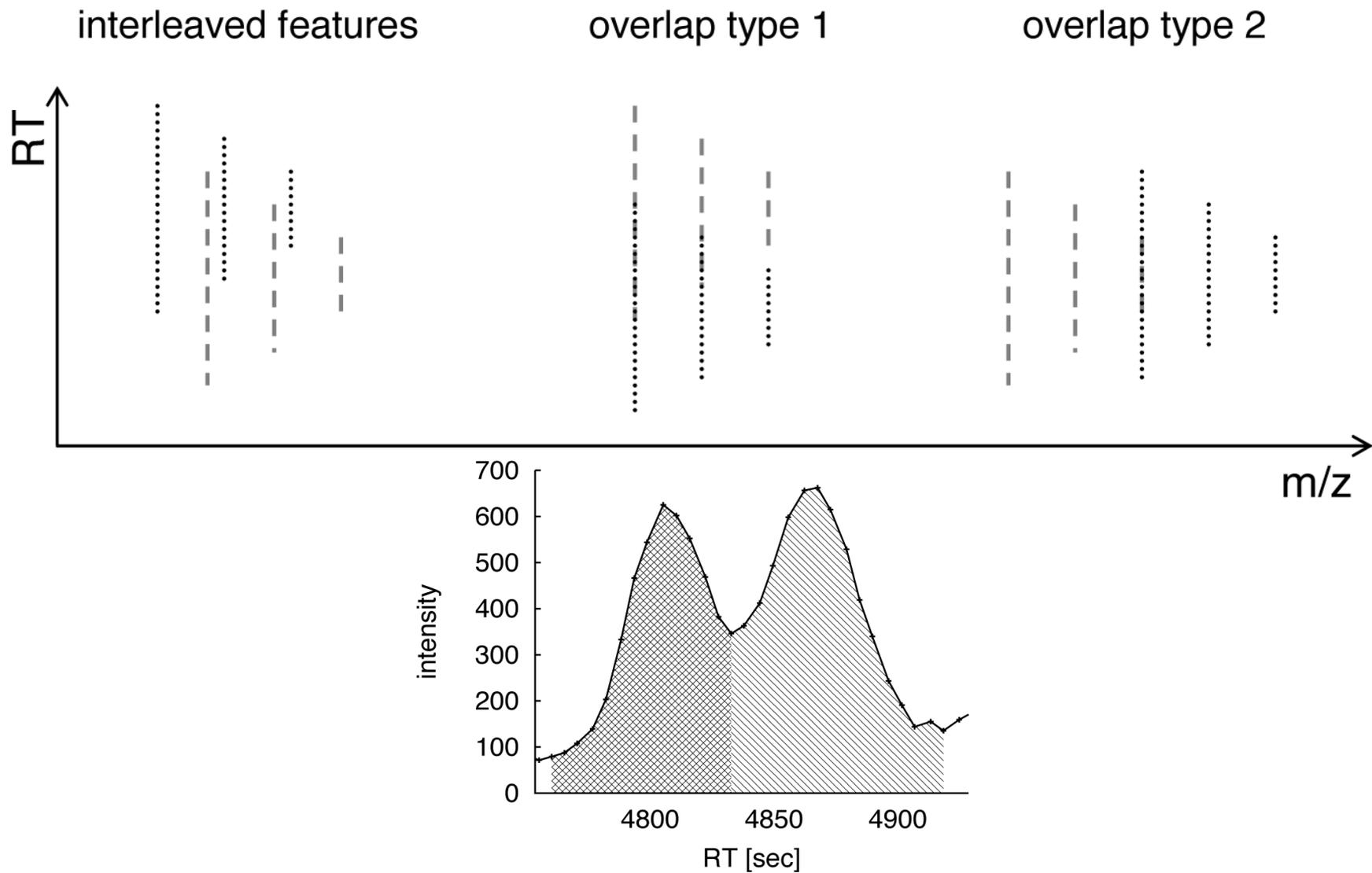
- A **mass trace** is a series of peaks along the RT dimension with little variation in the m/z dimension
- Mass traces are found with a simple heuristic aborting the search if the peak intensity hits the local noise level
- Search for mass traces in the correct m/z distance
- Limit length of mass trace to the length of the most intense mass trace



Feature Deconvolution

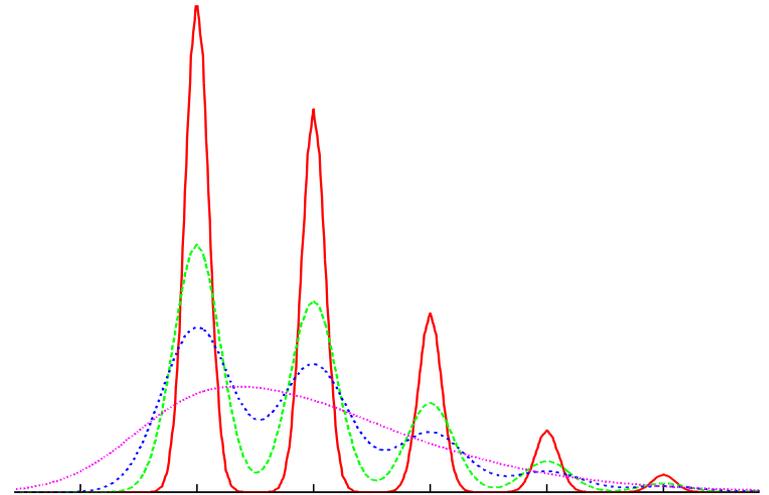
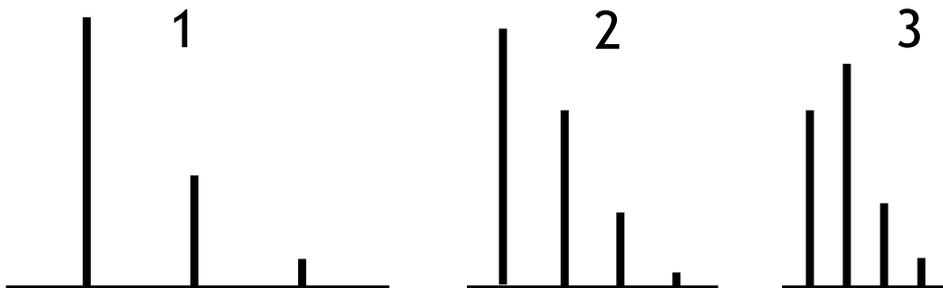
- Features can overlap in various ways
 - Mass traces can contain more than one chromatographic peak (features not baseline-separated in RT dimension)
 - Mass traces can be interleaved between features in the m/z dimension
 - Co-eluting features can be sharing mass traces
- Resolving these conflicts is done in a feature deconvolution step by statistical testing:
 - Test several hypotheses that could explain the features
 - The most likely of all hypotheses will be identified through comparison with the data

Feature Deconvolution



Algorithm: Modeling

- Test all possible models for different charges states (charge +2, charge +3, ...)
- Decide on the charge of the features based on the best fit for these models



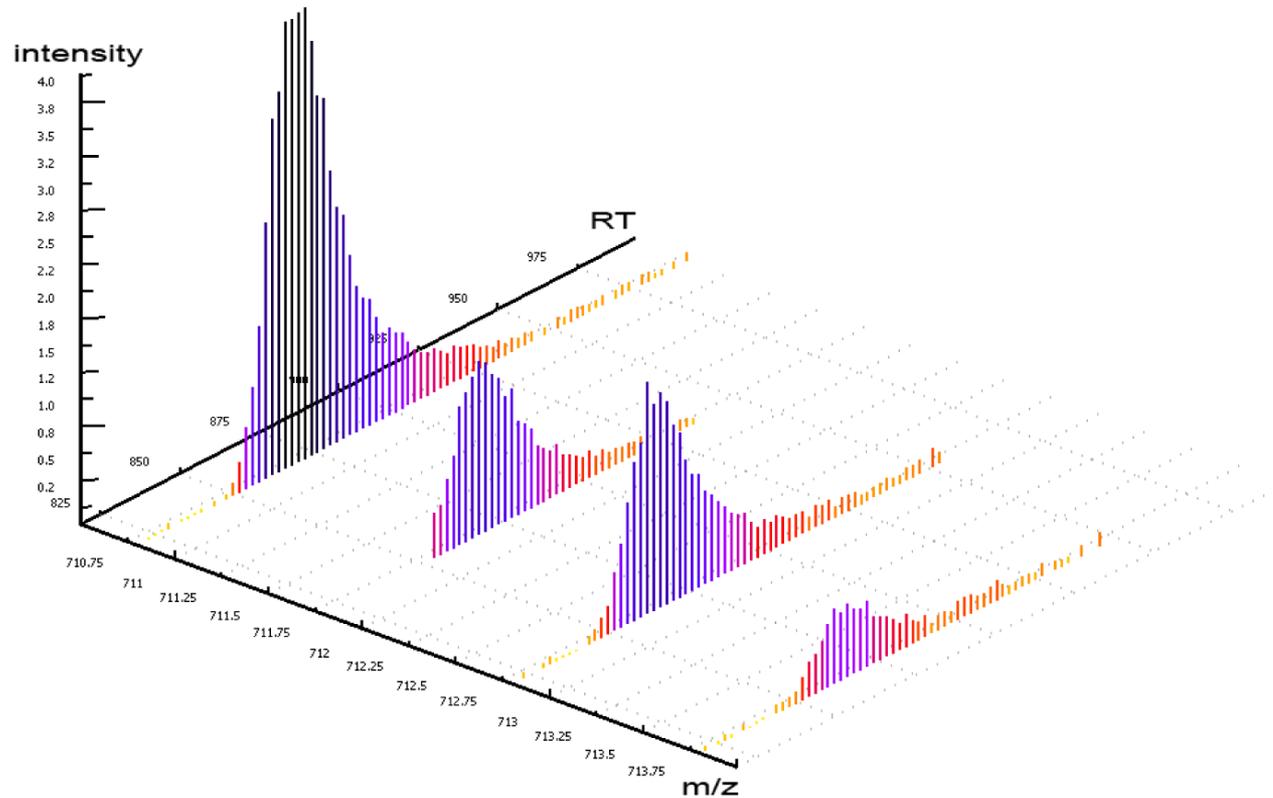
Algorithm: Modeling/Refinement

- Estimate **quality of fit** for model m and data d_i at positions r_i :

$$\text{fit}(m, d) = \frac{(\sum_i m(r_i) d_i)^2}{\sum m(r_i)^2 \sum d_i^2}$$

- Maximum Likelihood Estimator determines good **starting values for model parameters**
- **Further optimization of model parameters in refinement phase** (least-squares fit)

Feature Assembly



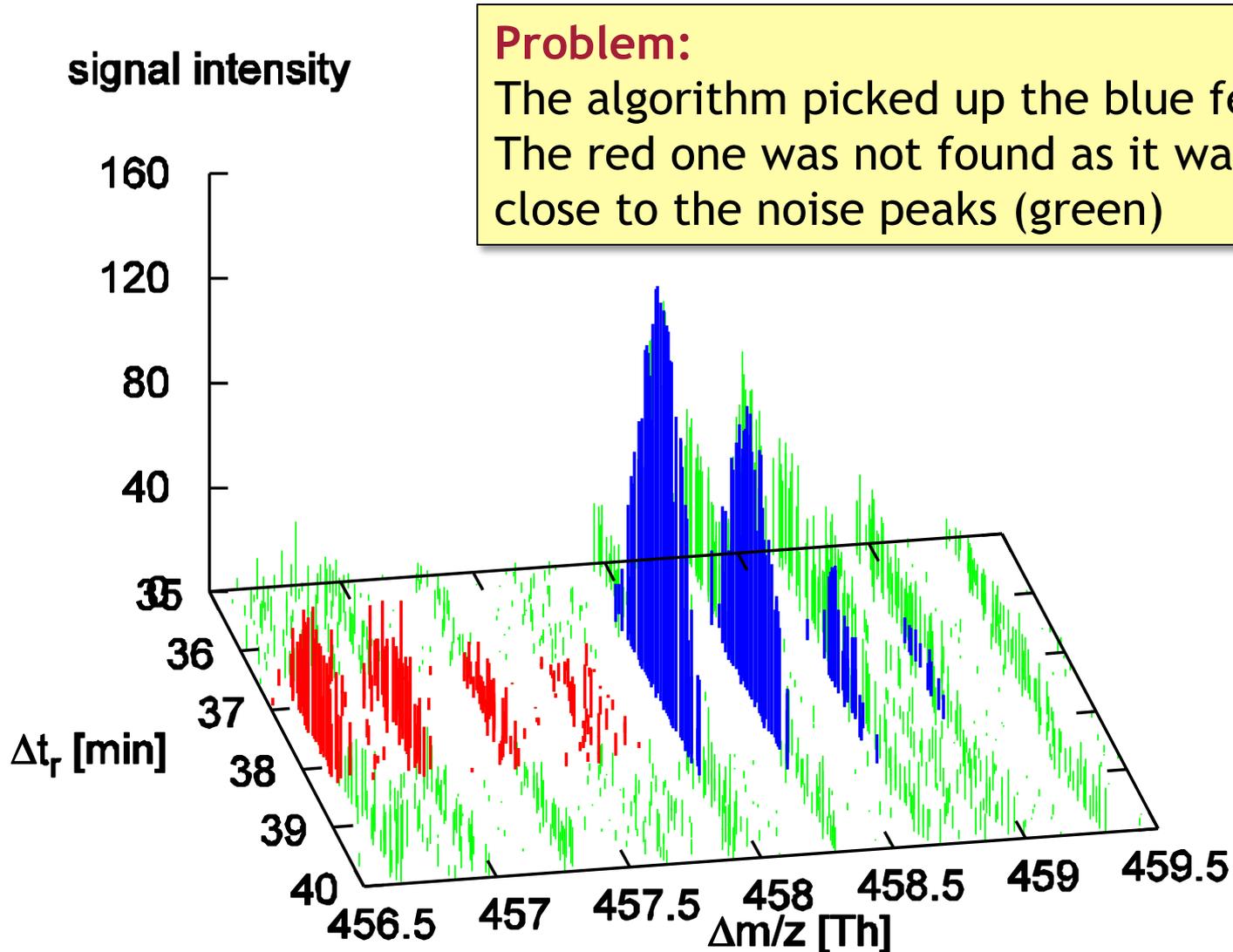
- Feature resolution is not always possible unambiguously

Feature Finding – Problems

Problems

- Low-resolution instruments might not yield good isotope patterns
- Peptides can overlap, in particular in complex samples
- Fitting of such overlapping patterns can yield bogus results
- Low-intensity features are hard to distinguish from noise peaks
- Isotope labels can skew the distributions or can lead to overlapping pairs

Still Difficult: Low-Intensity Features



LEARNING UNIT 5B

MAP ALIGNMENT

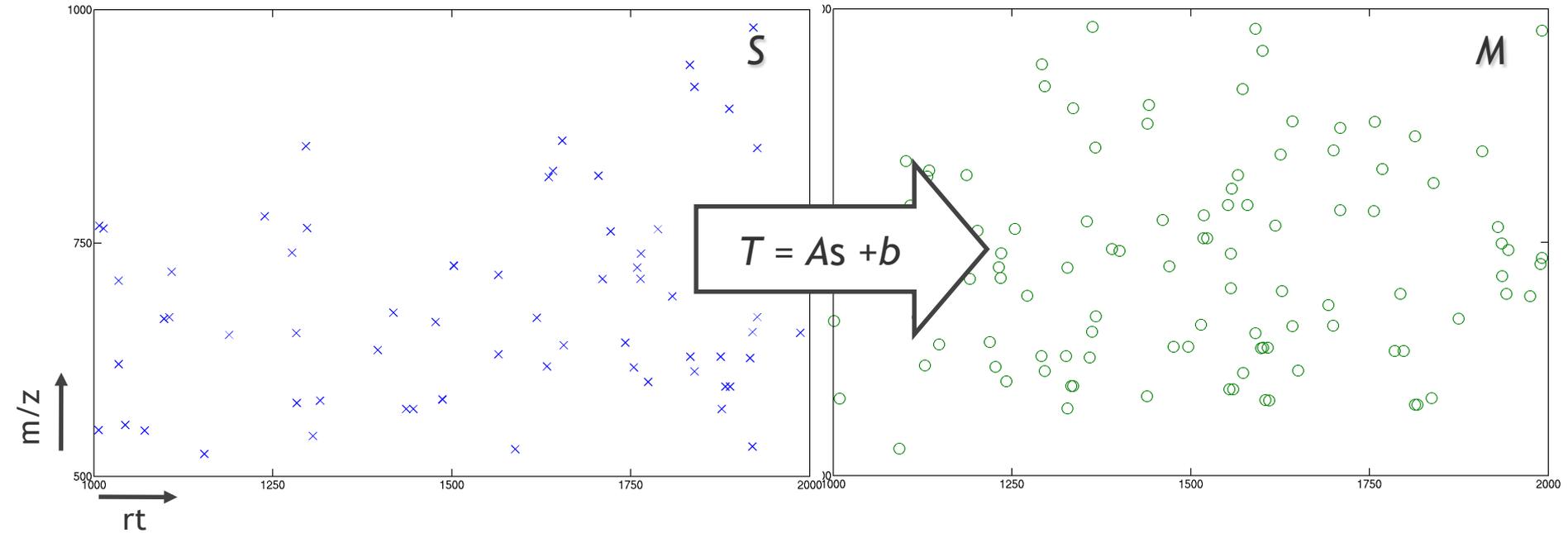
Map alignment

- Problem definition
- Pose-clustering algorithms
- Dynamic time-warping techniques
- Map alignment and feature linking
- Map normalization

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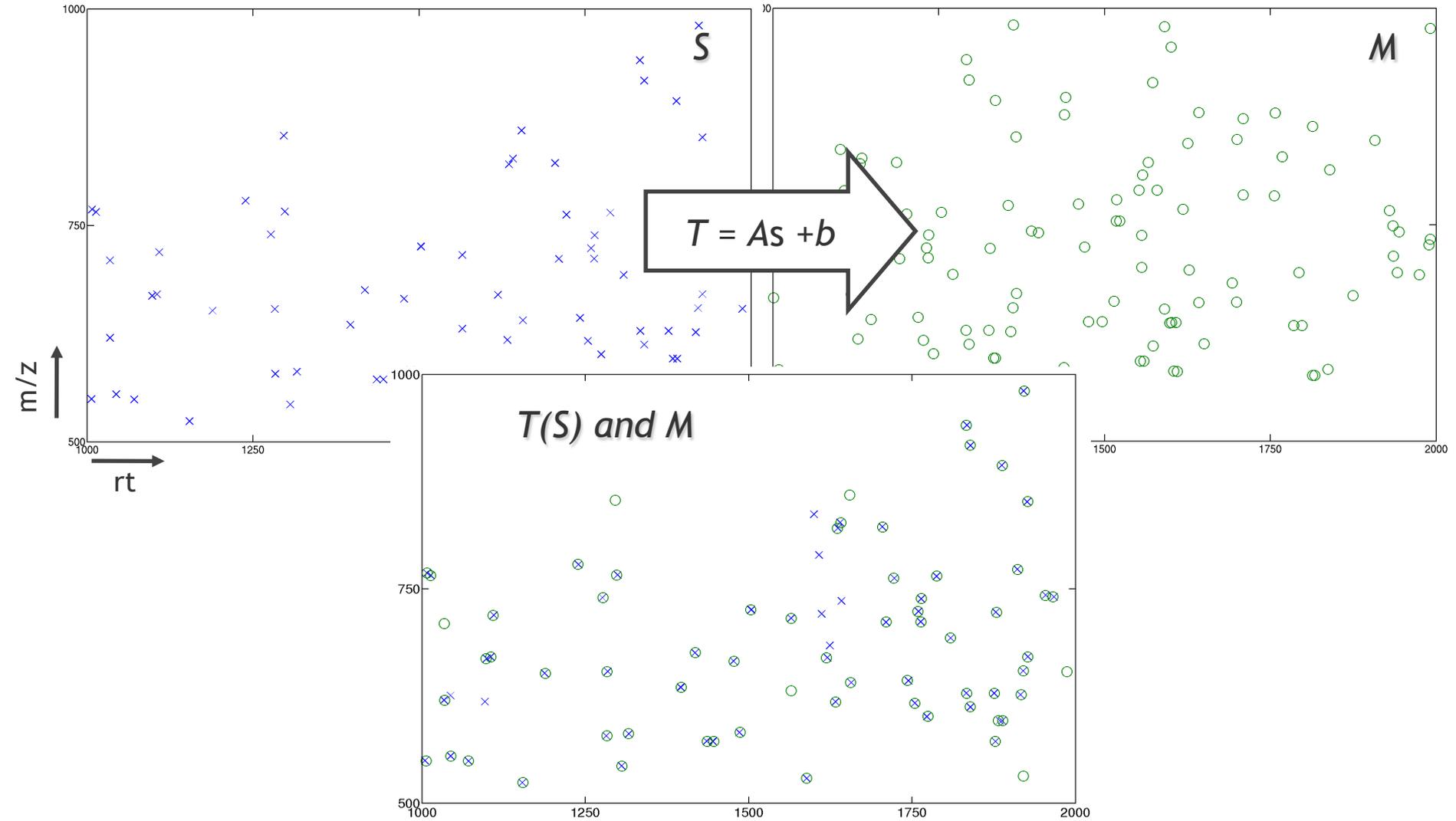


Pairwise Alignment

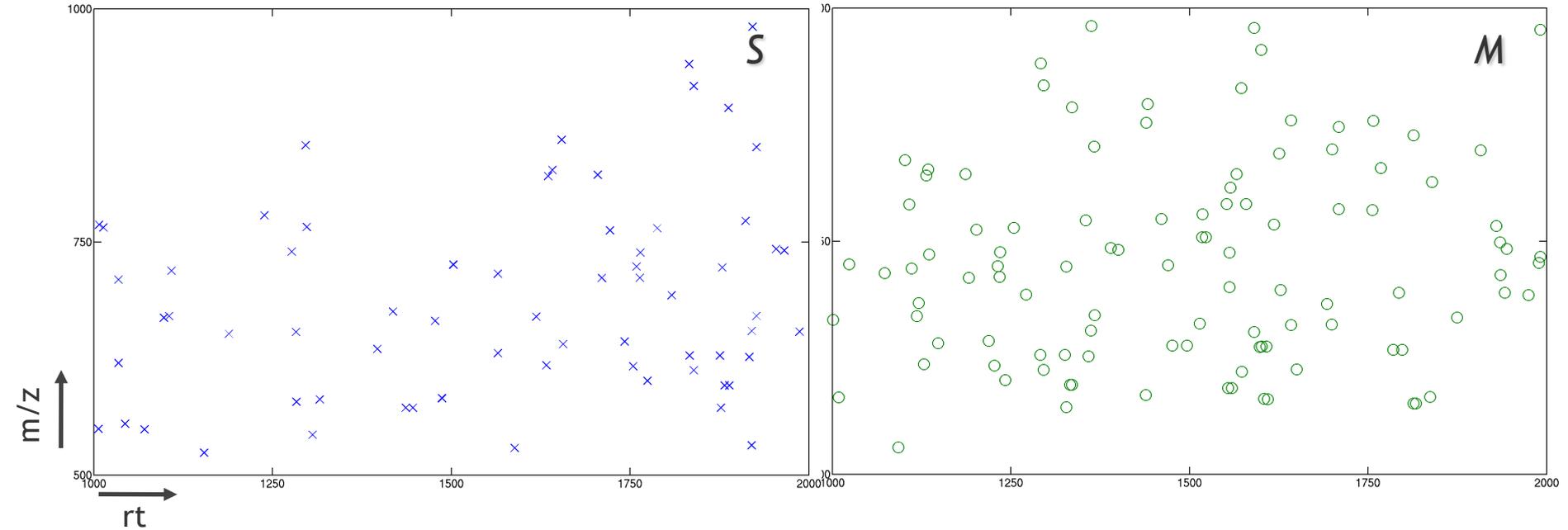


The problem is to find the affine transformation T that minimizes the distance between $T(S)$ and M .

Pairwise Alignment



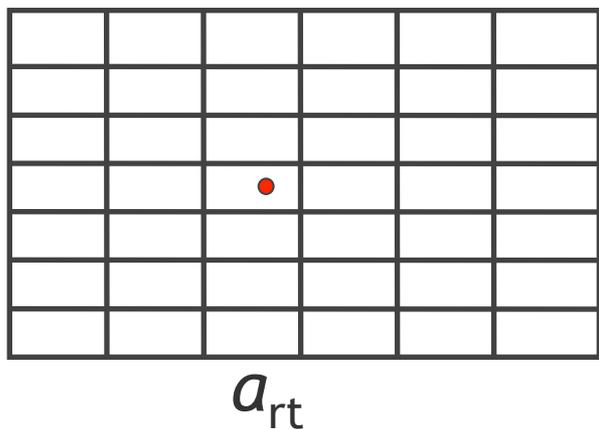
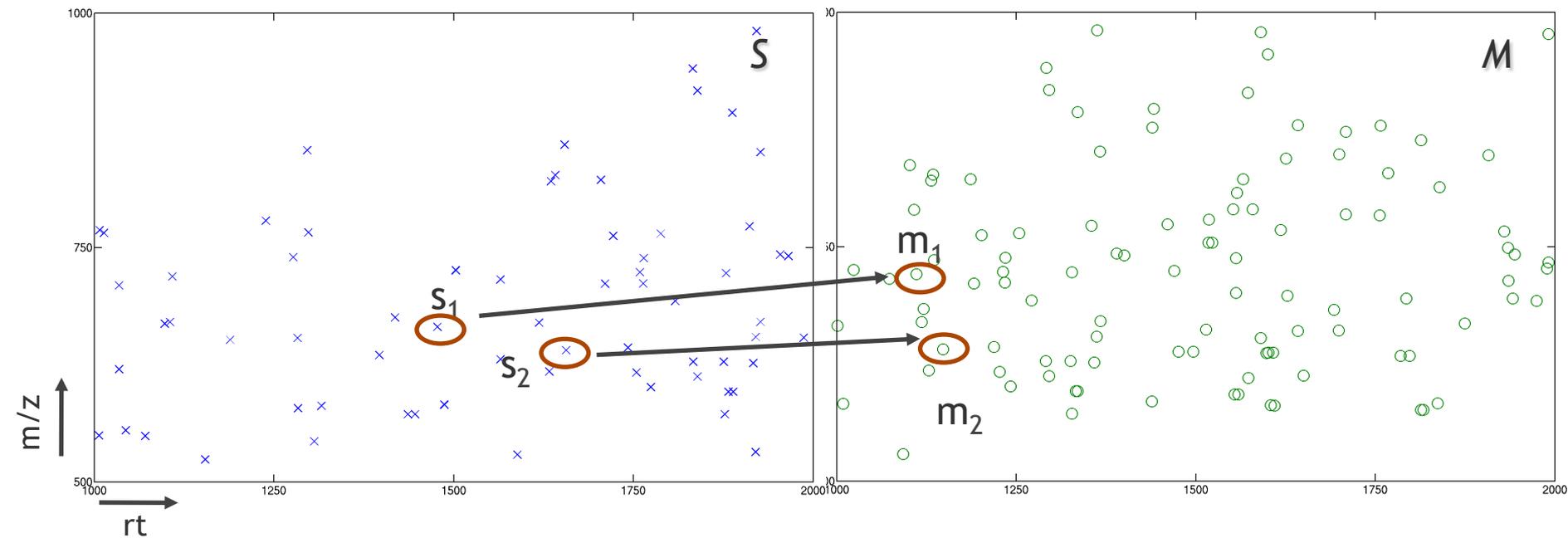
Pose Clustering



$$T_{rt}(s_{rt}) = a_{rt}s_{rt} + b_{rt}$$

$$T_{m/z}(s_{m/z}) = a_{m/z}s_{m/z} + b_{m/z}$$

Pose Clustering

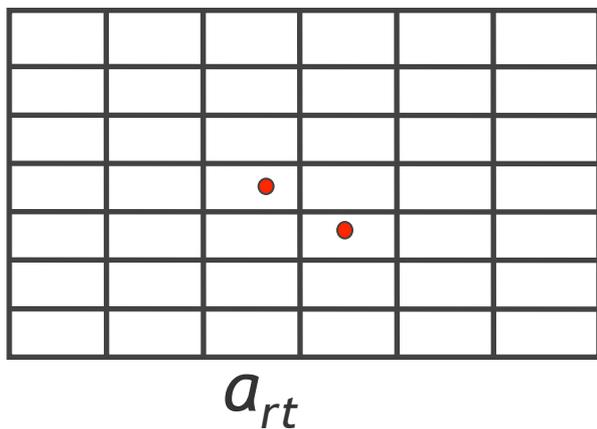
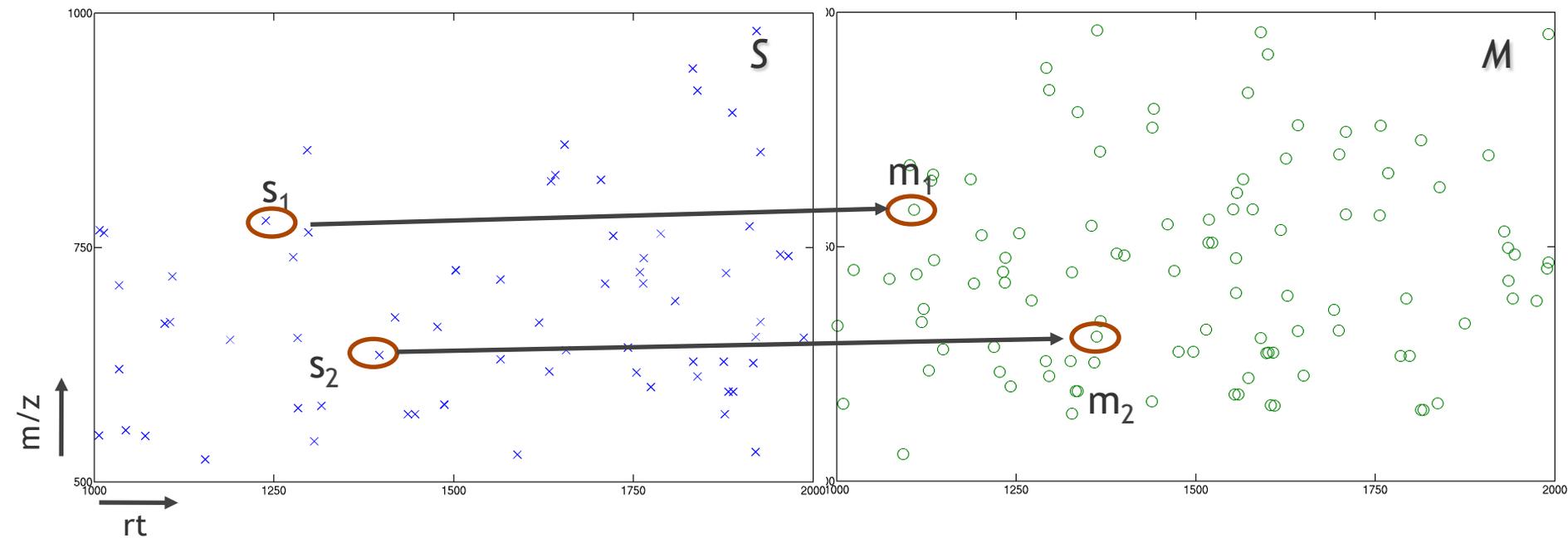


b_{rt}

$$m_1 = a_{rt}s_1 + b_{rt}$$

$$m_2 = a_{rt}s_2 + b_{rt}$$

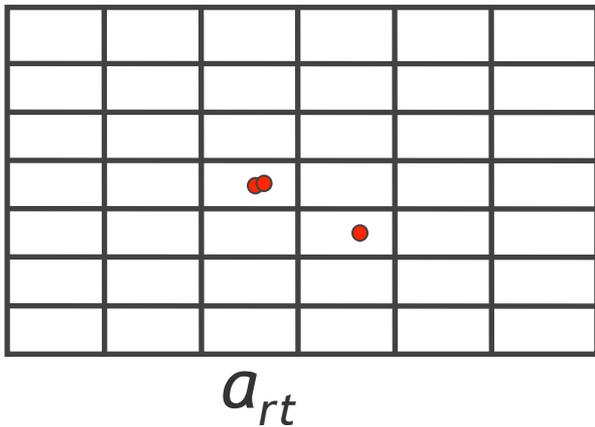
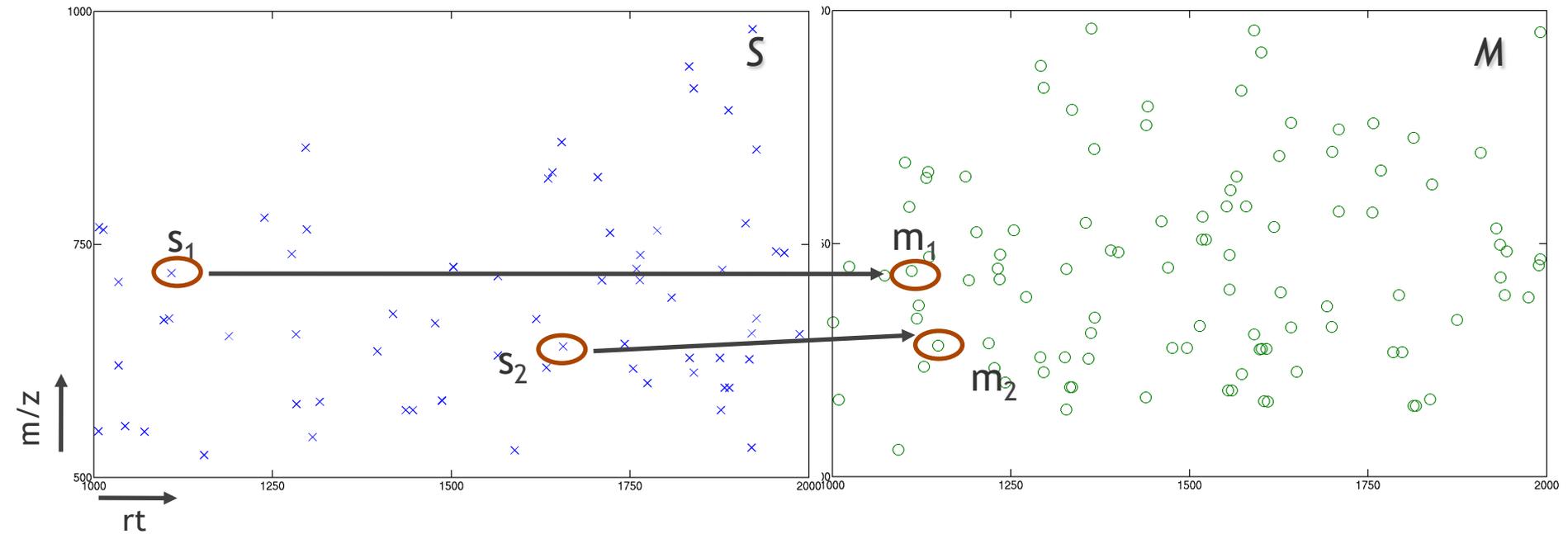
Pose Clustering



$$m_1 = a_{rt}s_1 + b_{rt}$$

$$m_2 = a_{rt}s_2 + b_{rt}$$

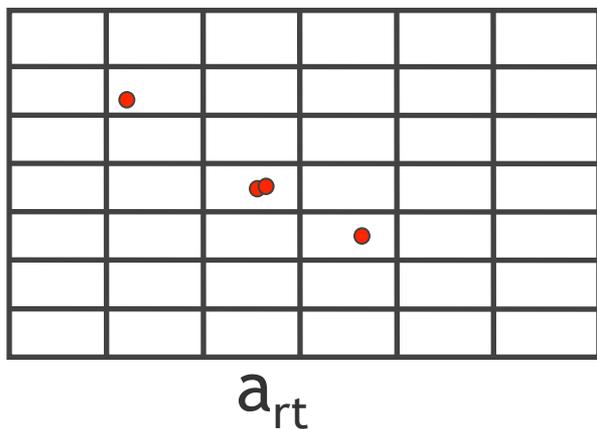
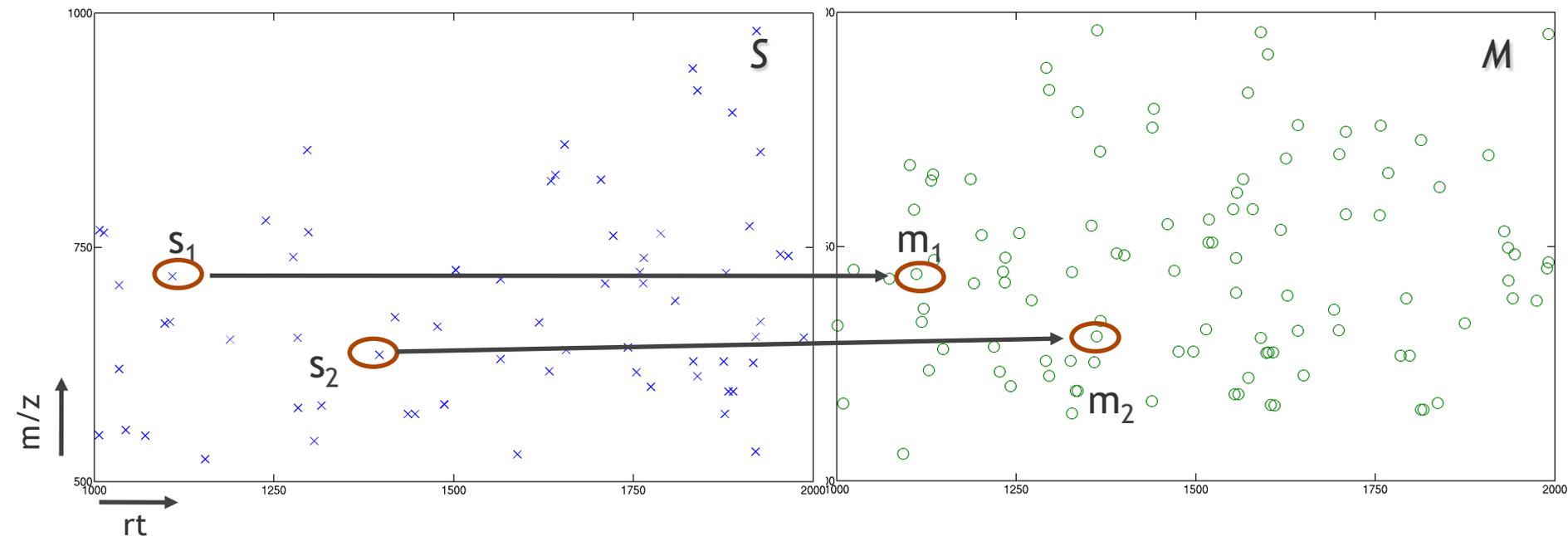
Pose Clustering



$$m_1 = a_{rt}s_1 + b_{rt}$$

$$m_2 = a_{rt}s_2 + b_{rt}$$

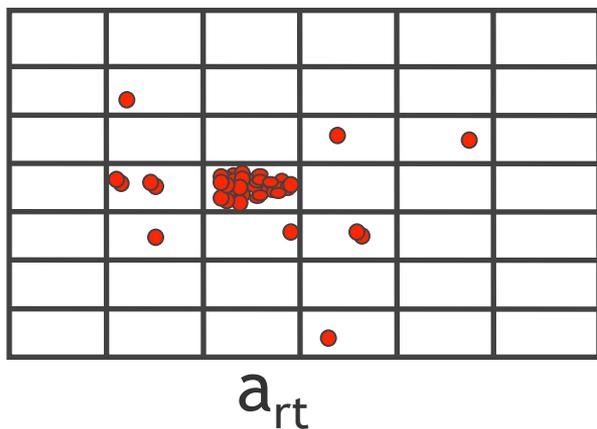
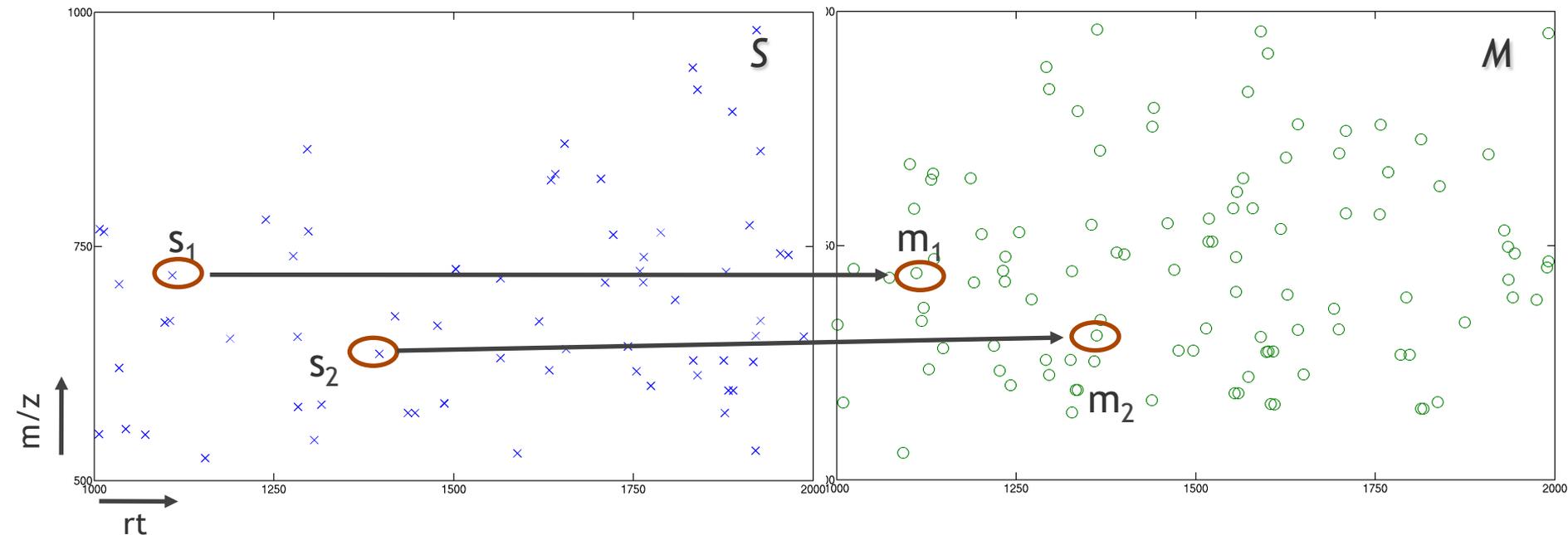
Pose Clustering



$$m_1 = a_{rt}s_1 + b_{rt}$$

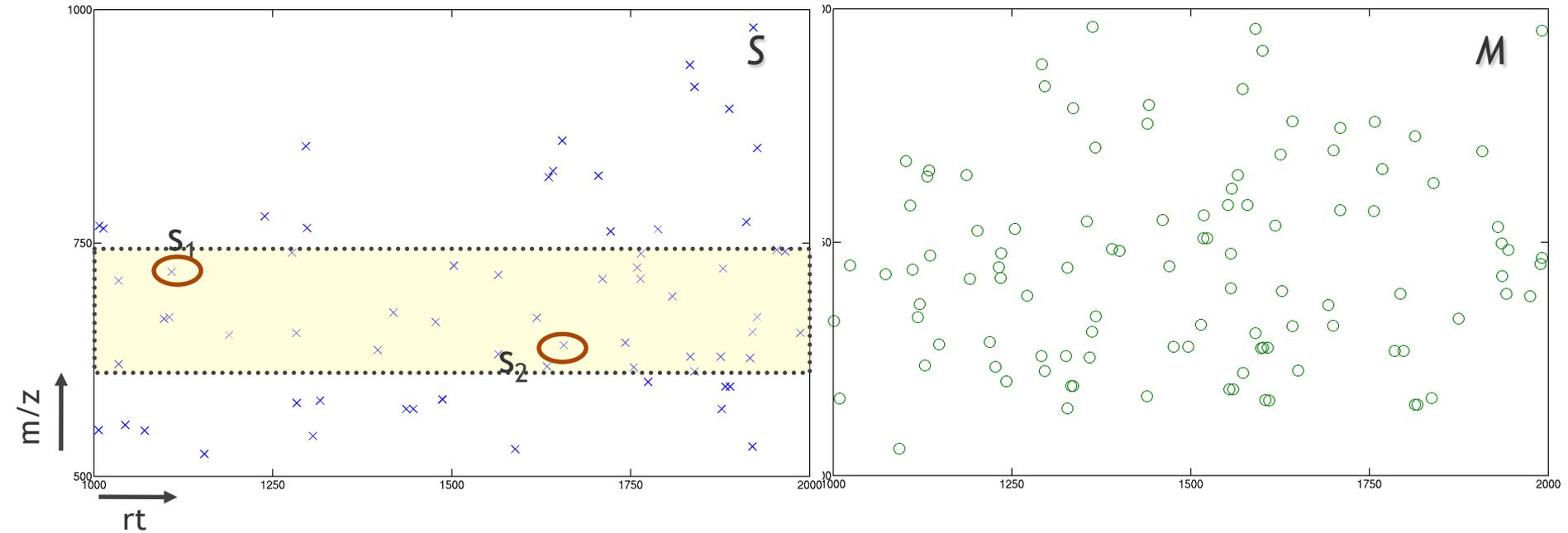
$$m_2 = a_{rt}s_2 + b_{rt}$$

Pose Clustering



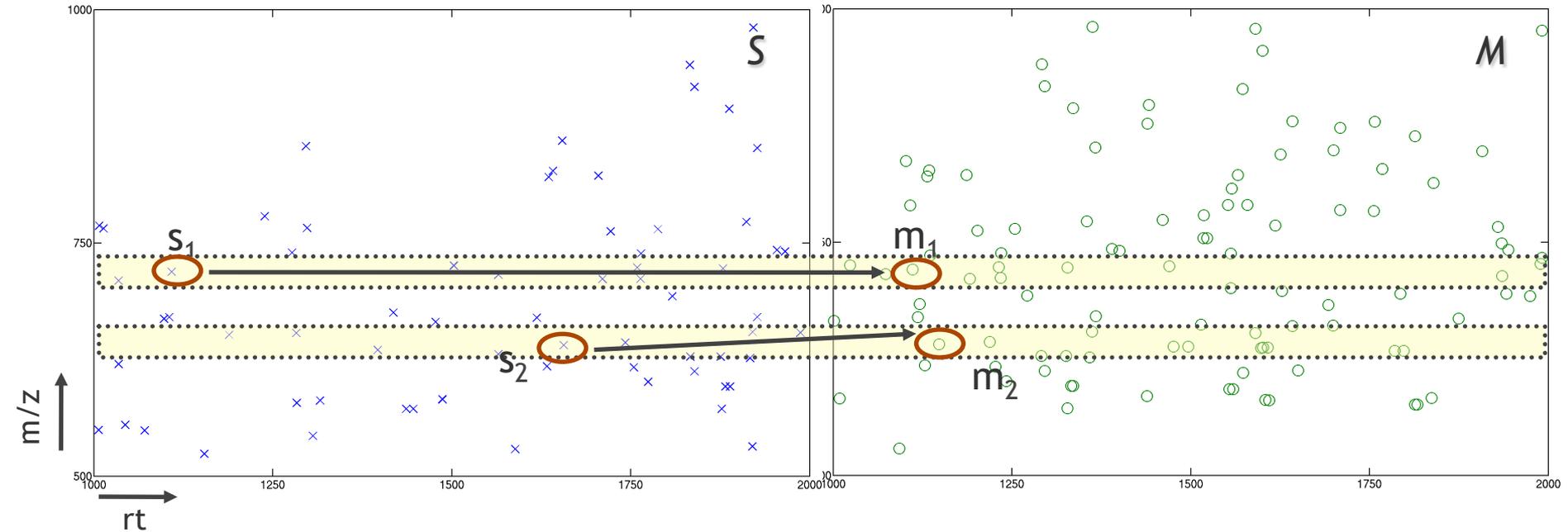
- Matching of corresponding pairs will result in the correct transformation
- These are more likely than random matches!

Speeding Things Up



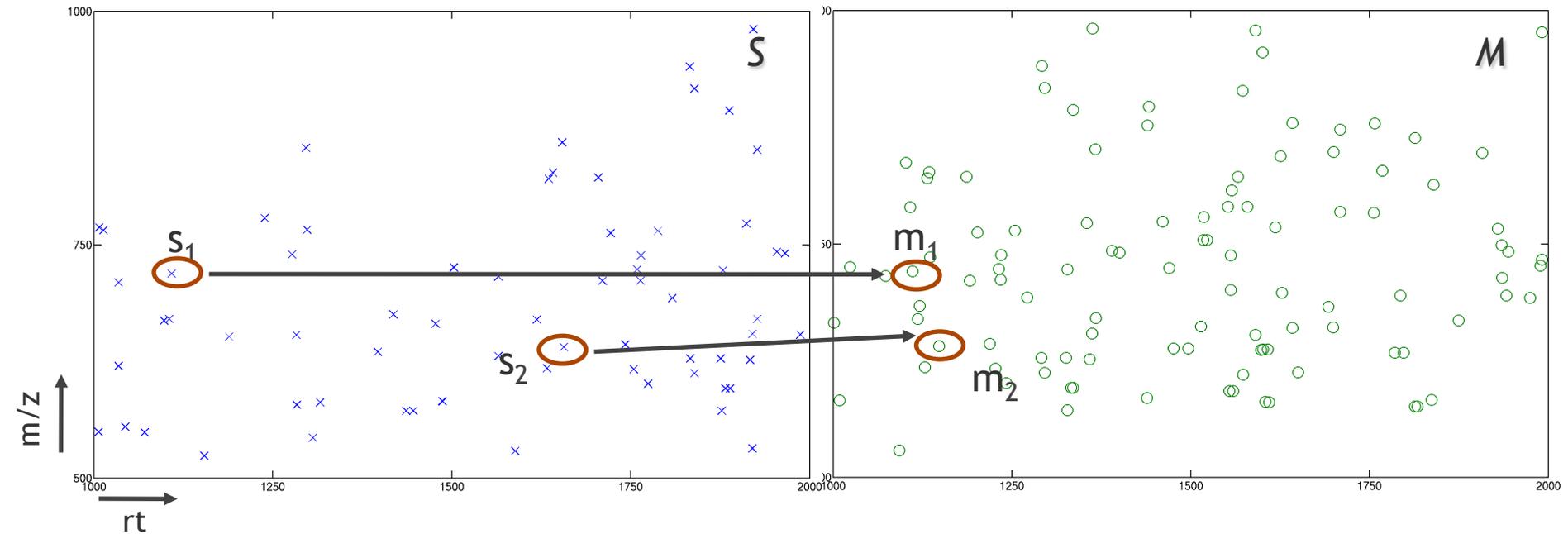
Only consider pairs (s_1, s_2) in S with s_1 having a small distance to s_2 in m/z .

Speeding Things Up



Only match
pair (s_1, s_2) onto pair (m_1, m_2)
if s_1 and m_1 as well as s_2 and m_2
lie close together in m/z .

Improve Matching



Normalize intensities in M and S :
weight the vote of each transformation
by the intensity similarities of the
point matches (s_1, m_1) and (s_2, m_2) .

Linear Alignment

- Podwojski *et al.* proposed an alternative linear alignment method and also extended this to a nonlinear alignment
- The linear alignment is similar to the algorithm by Lange *et al.*
- It uses a different type of cluster analysis to determine a linear regression
- In contrast to the Lange algorithm, it generalizes nicely to multiple map alignment

Preliminaries

combine all n LC/MS runs

build overlapping mass-windows across combined runs

1. Cluster Analysis

for each mass-window do

use p peaks with highest intensities

calculate distance matrix of pairs of peaks (j, h)

$$d_{j,h} = \begin{cases} \text{diff}(mass), & \text{if } \text{diff}(rt) < k_1 \wedge \\ & \text{diff}(\log_{10}(intensity)) < k_2 \\ \infty, & \text{if } \text{diff}(rt) \geq k_1 \vee \\ & \text{diff}(\log_{10}(intensity)) \geq k_2 \end{cases}$$

hierarchical average linkage cluster analysis

cut cluster-tree at mass accuracy Δ_m

if $n_{dup} < threshold_1 \wedge n_{miss} < threshold_2$ **then**
cluster is 'well-behaved'

delete duplicated 'well-behaved' clusters

for each 'well-behaved' cluster **do**

$\tilde{rt} = \text{median}(rt)$

for each peak i **do**

$$dev_i = rt_i - \tilde{rt}$$

2. Regression

for each run s **do**

take only peaks from 'well-behaved' clusters

fit regression line $\hat{dev}_{s,i} = a_s + b_s * rt_i$

by minimizing $\sum (dev_i - \hat{dev}_{s,i})^2$

Correction

for each run s **do**

for each peak i **do**

$$rt_{cor,i} = rt_i - \hat{dev}_{s,i}$$

Nonlinear Alignment

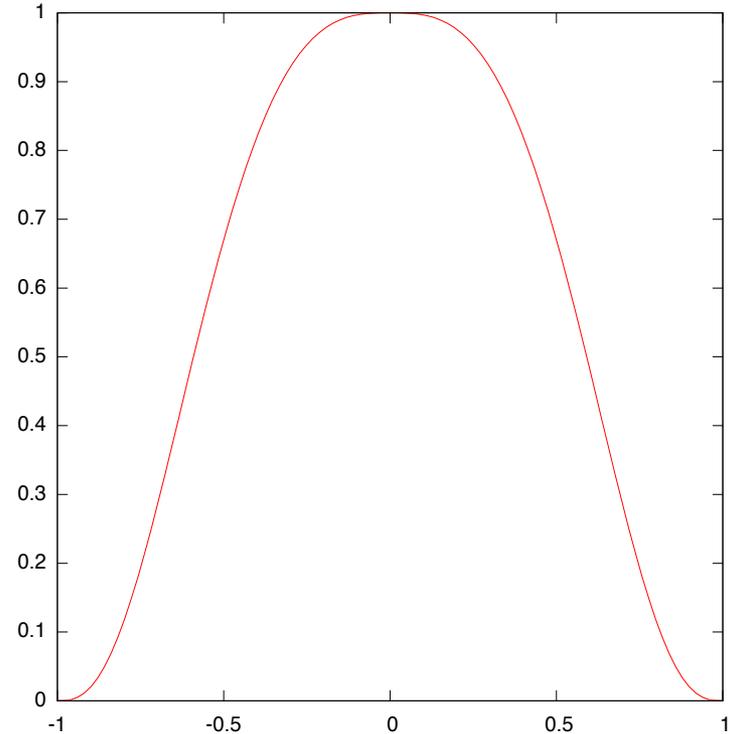
- **Idea**
 - Perform linear alignment (using pose clustering)
 - Compute a more accurate local alignment using LOESS regression
- **LOESS regression** (often also called LOWESS)
 - Locally weighted polynomial regression
 - Based on a pre-defined window size
 - Points within this window contribute to the local regression
 - Perform local regression (linear or quadratic, cubic) around the predicted coordinate

LOESS Regression

- Weighting is often performed by tricubic weighting function

$$w(z) = \begin{cases} (1 - |z|^3)^3 & \text{if } |z| < 1 \\ 0 & \text{otherwise} \end{cases}$$

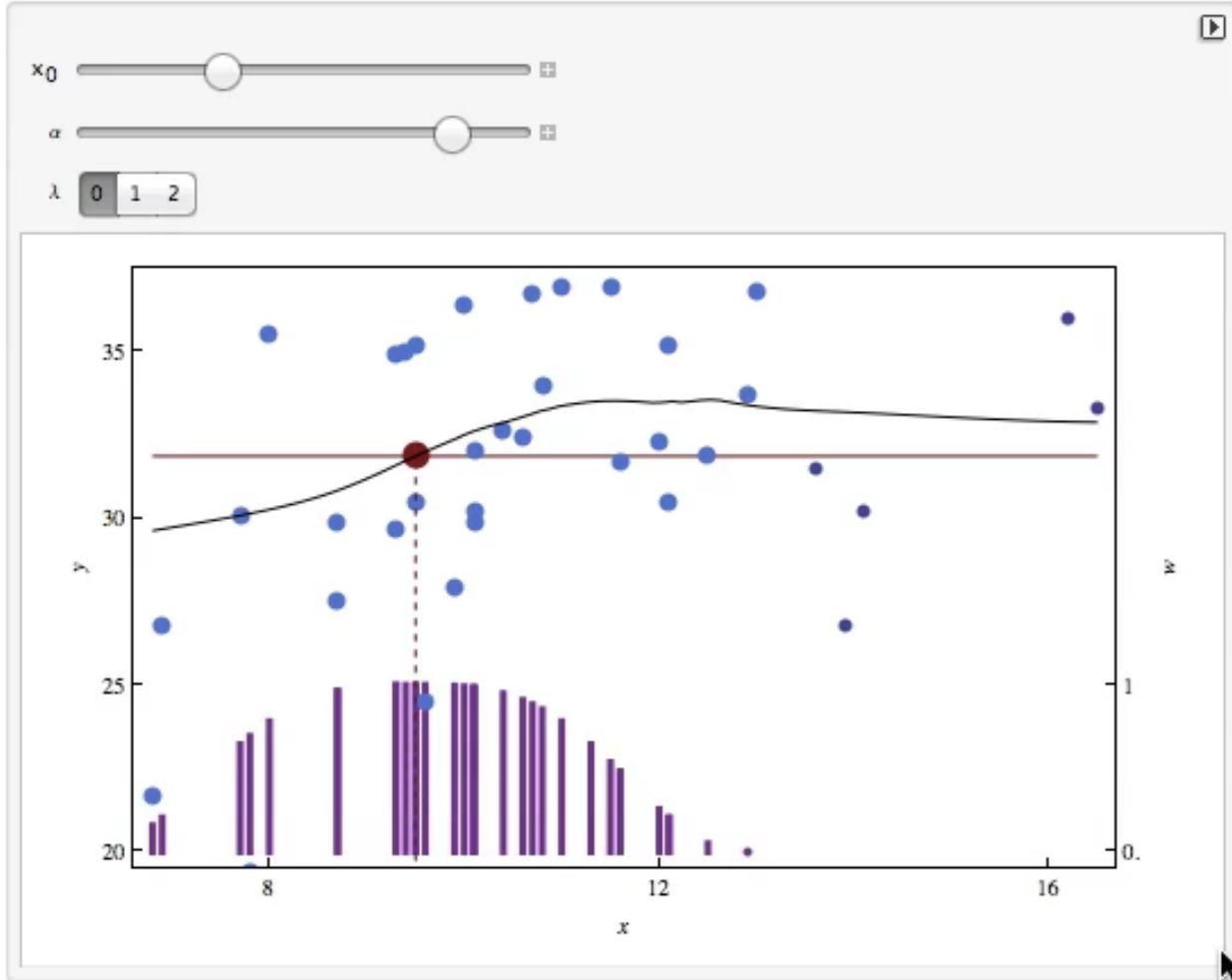
- Weighting function is applied to coordinates scaled into the chosen window (-1 · 0 · 1)
- Local regression (linear quadratic) needs to be recomputed around every point (computationally very expensive)



tricubic function

LOESS Regression

How Loess Works

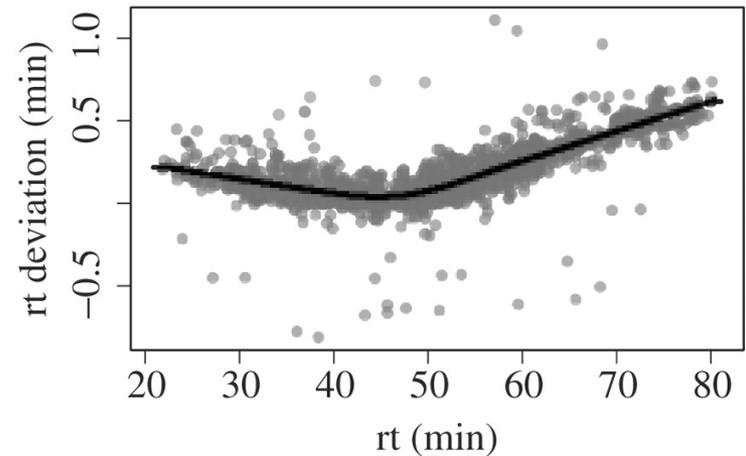
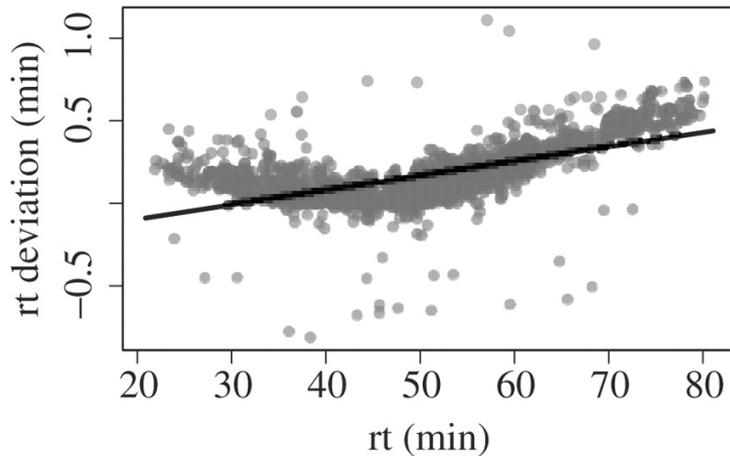
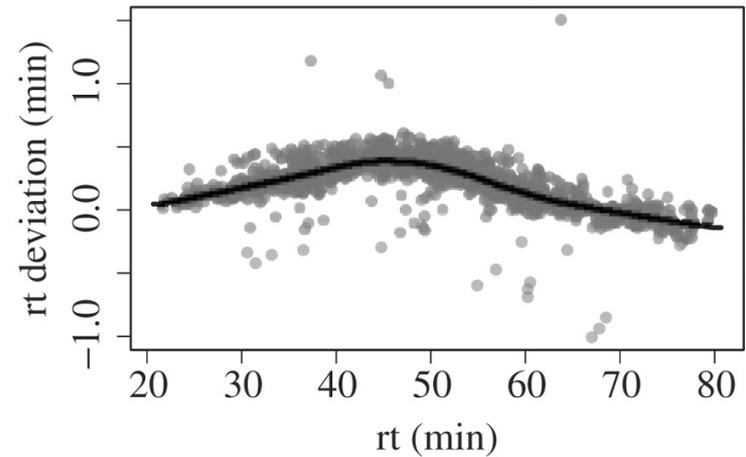
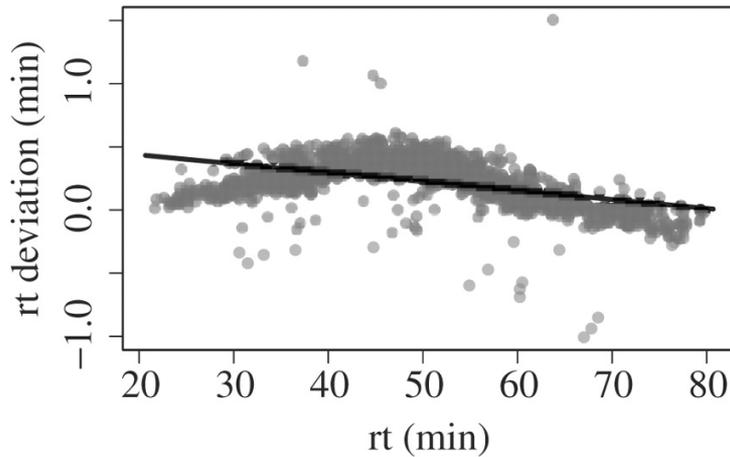


For $0 < \alpha \leq 1$

$[\alpha \cdot n]$
nearest neighbours
are considered

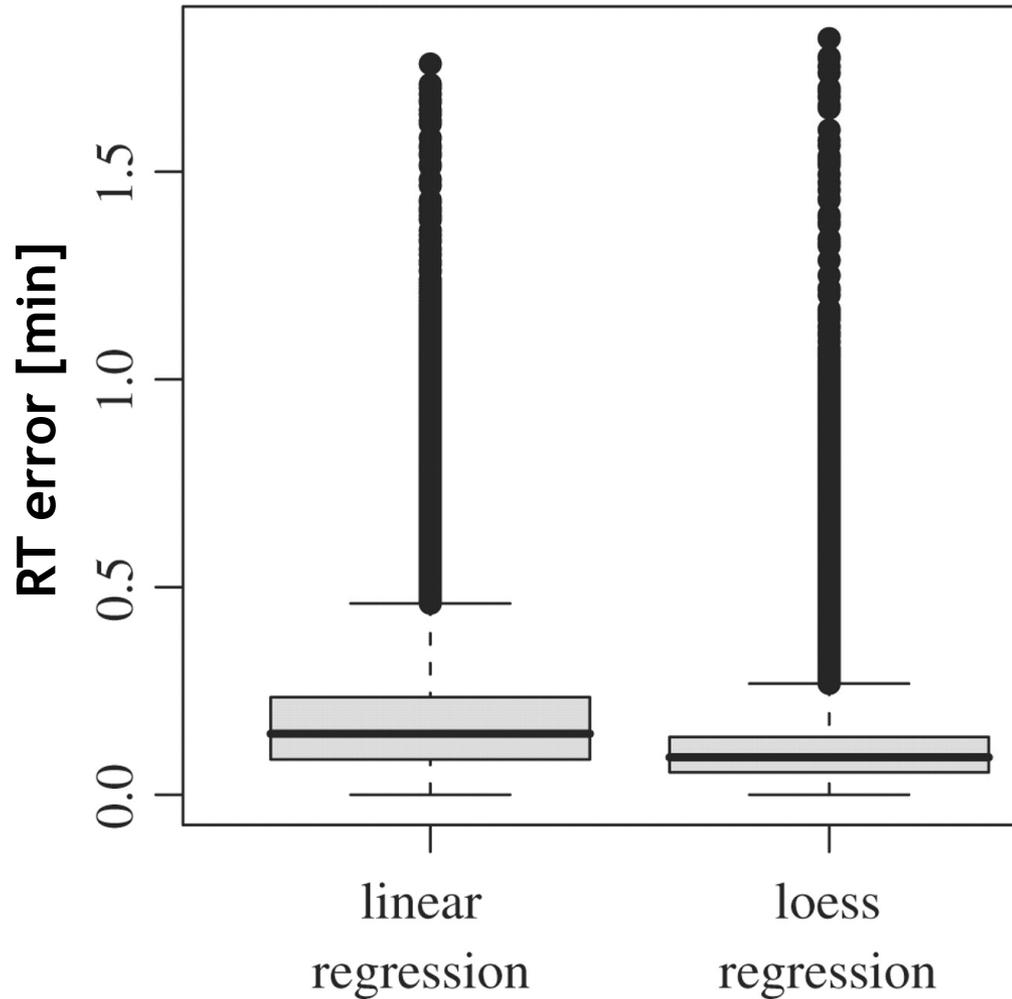
λ
gives degree of
fitted polynomial

Nonlinear Alignment



**Alignment of two different datasets (top/bottom). Left: linear, right: nonlinear.
(around 30 k aligned peaks)**

Nonlinear Alignment



Comparison of median RT error for linear/nonlinear regression

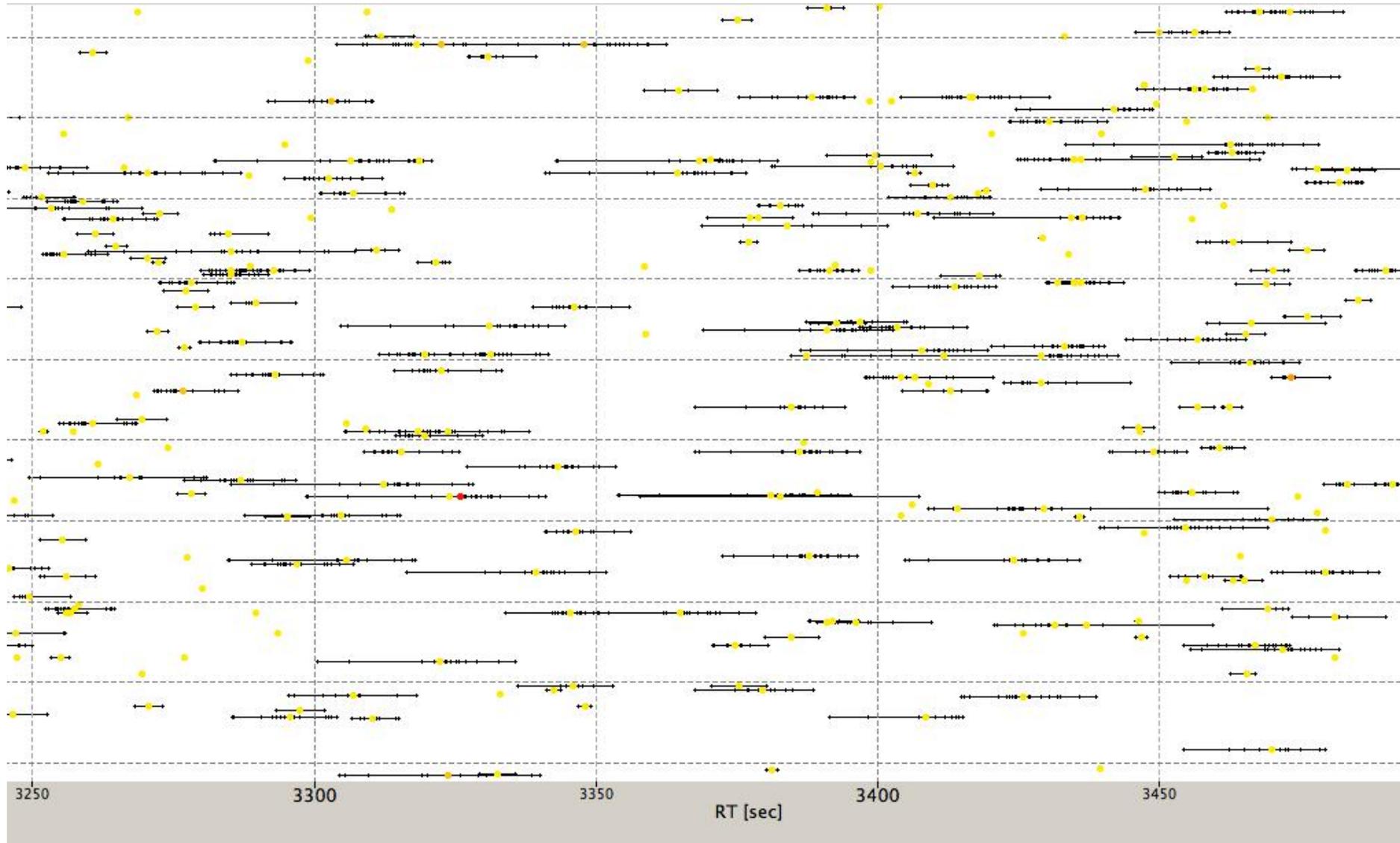
Feature Linking

- Map alignment does not yet create a direct correspondence (bijection) between the features!
- Feature linking pairs up features
 - **across maps** for label-free quantification
 - **within maps** for arbitrary labeling strategies (e.g., SILAC: link pairs 6 Da apart)
- A user-specified **mass tolerance** and **retention time tolerance** are required as input
- Labeled feature linking also requires the specification of the label distance (mass difference)
- The result are consensus features containing the original features as well
- Correctness of linked features can also be verified through identifications (if present)

OpenMS/TOPP

- OpenMS implements the Lange et al. algorithm
- TOPP contains tools for map alignment and for feature linking
 - MapAlignerPoseClustering
 - Implements the pose clustering algorithm and computes the corresponding transformation
 - FeatureLinkerUnlabeledQT
 - Uses QT clustering to compute the best assignment of features across several maps
 - Result is a consensus map

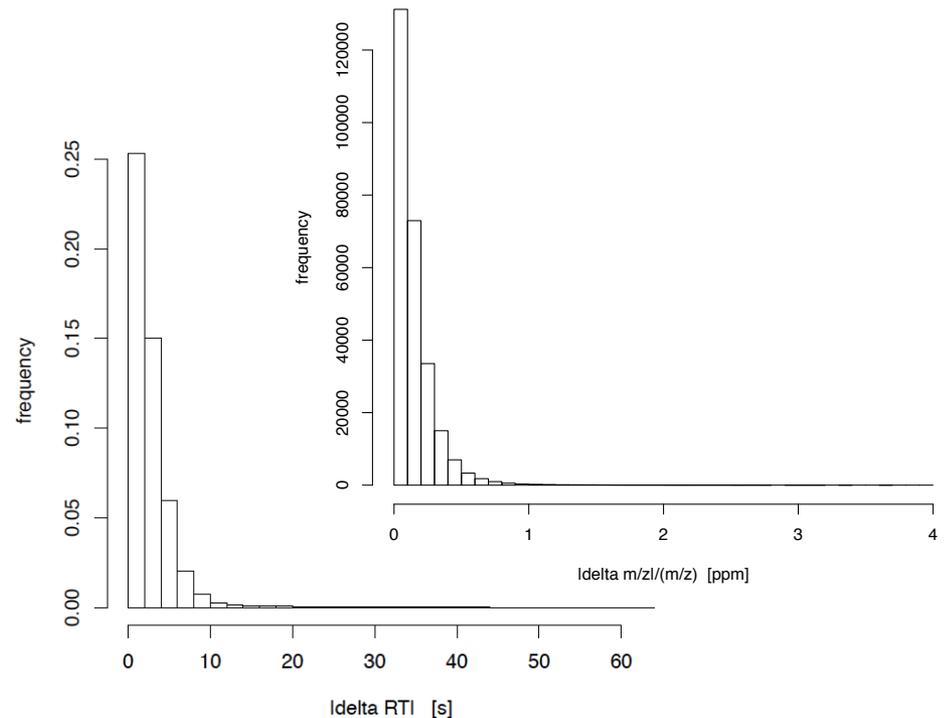
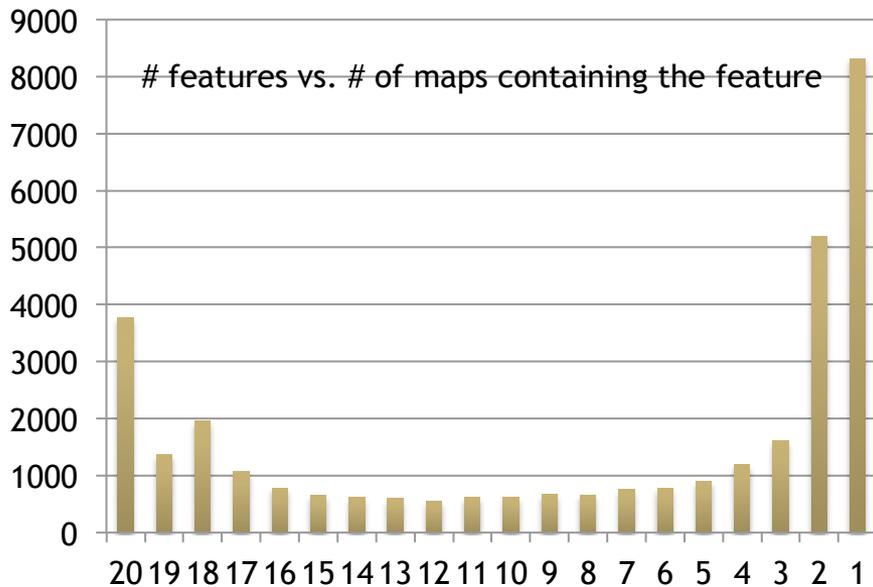
Consensus Features



Quality Control

- **MapStatistics**

- Produces some descriptive statistics of a map for QC
 - Did feature finding and map alignment work properly?
 - Do all maps we aligned have roughly the same amount of features?
 - Check instrument calibration and stability of chromatography

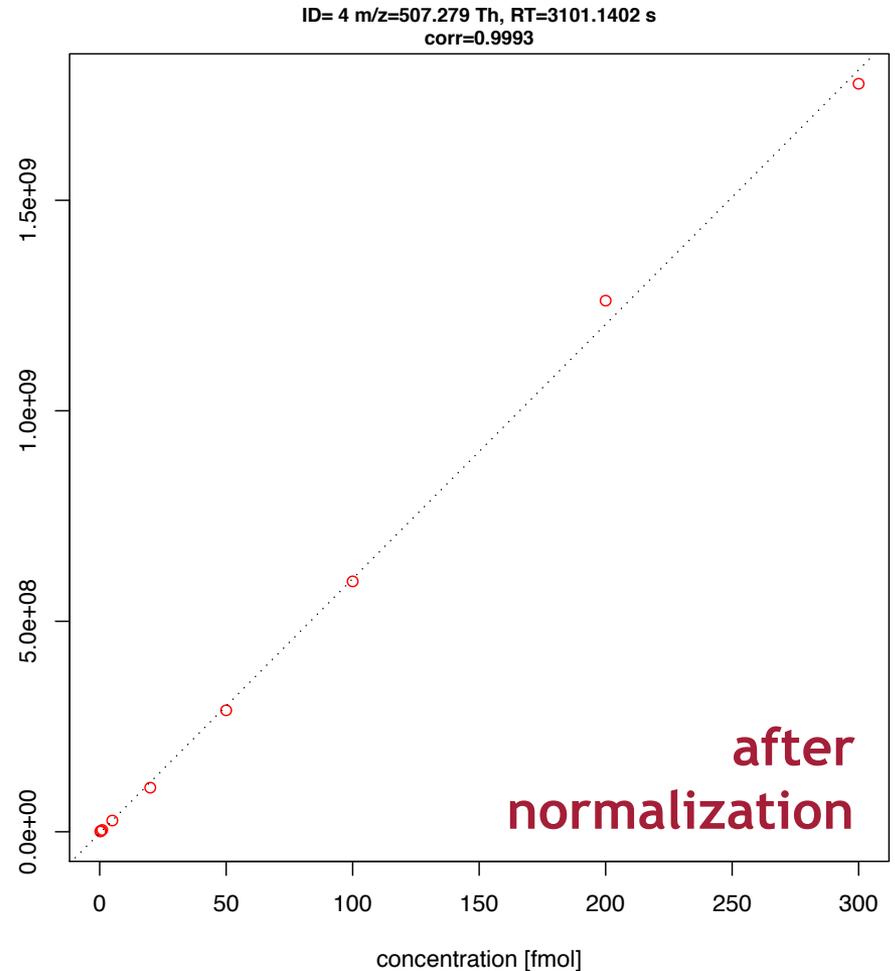
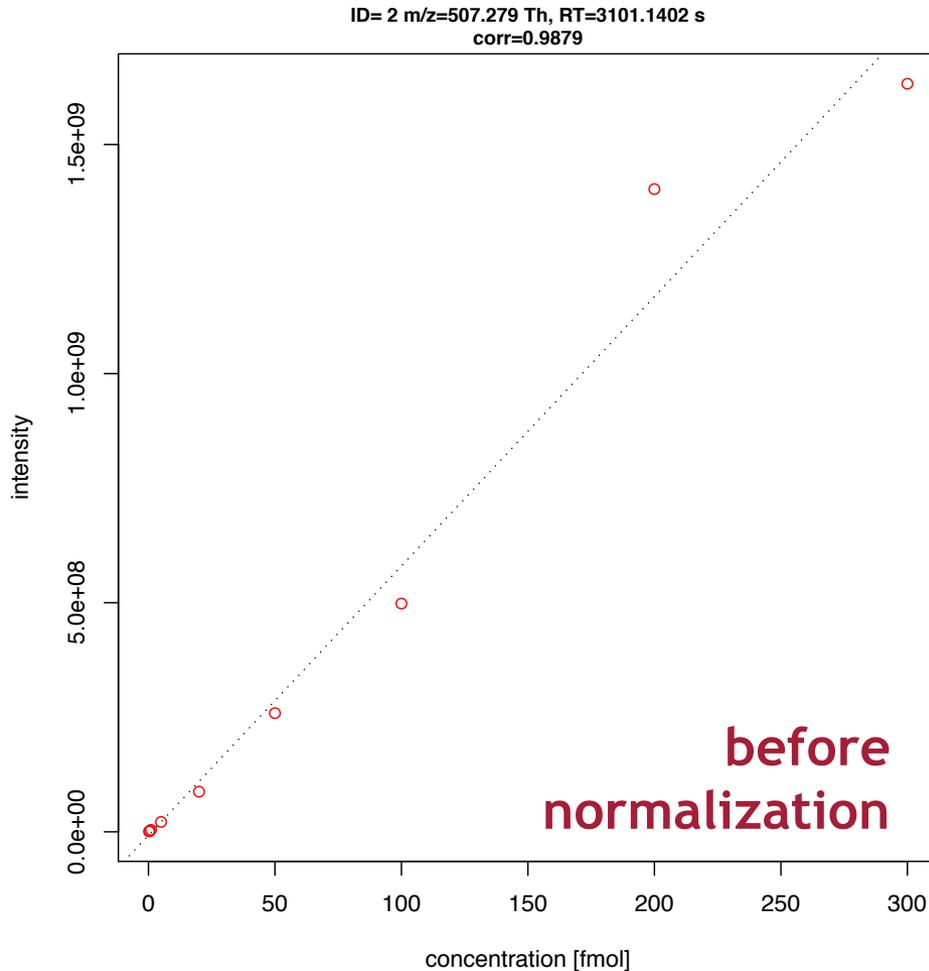


Map Normalization

- For label-free quantification a normalization of features across maps is often helpful
- **Strategy 1: internal standards**
 - Spiked in peptides/proteins are used for normalizing maps
 - This is easily done in a statistics package or Excel after the analysis
- **Strategy 2: background normalization**
 - For a sufficiently complex background only a small number of features/peptides will be differential
 - The background can be used to normalize maps with respect to each other (keeping the ration of unregulated background features at 1:1)
- **Idea: 'robust regression'**
 - Look at all the ratios
 - Remove outliers
 - Determine the normalization factor from the rest

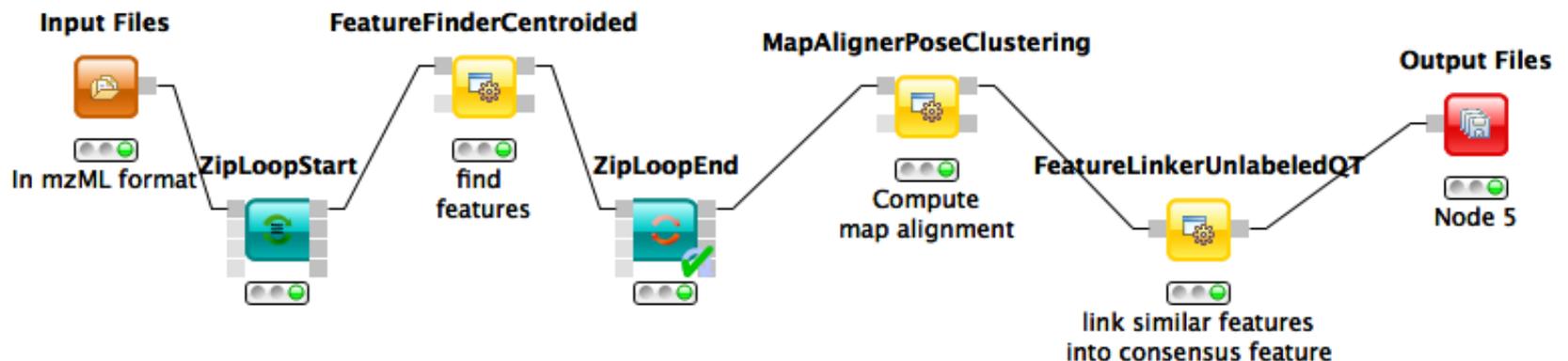
Effect of Normalization

- Label-free quantification in a complex (platelet) background measured with a spiked in peptide



Feature Finding in KNIME

- TOPP tool FeatureFinder
(FeatureFinderCentroided in OpenMS 1.11)
- Reads a centroided LC-MS map – so if data is available as raw data, it needs to be converted to centroided data using a peak picker
- Label-free workflows can get rather complicated and usually require identification steps as well (which we will discuss later in the lecture)



LEARNING UNIT 5C

SILAC QUANTIFICATION

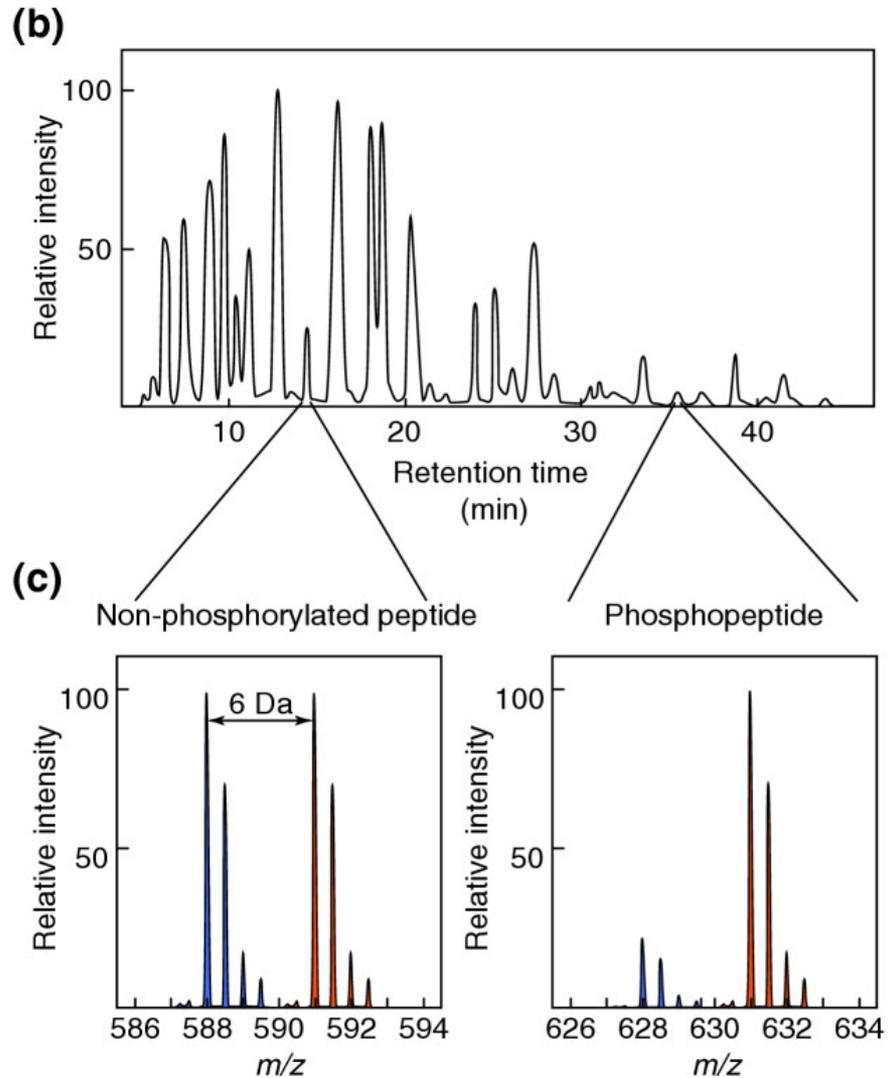
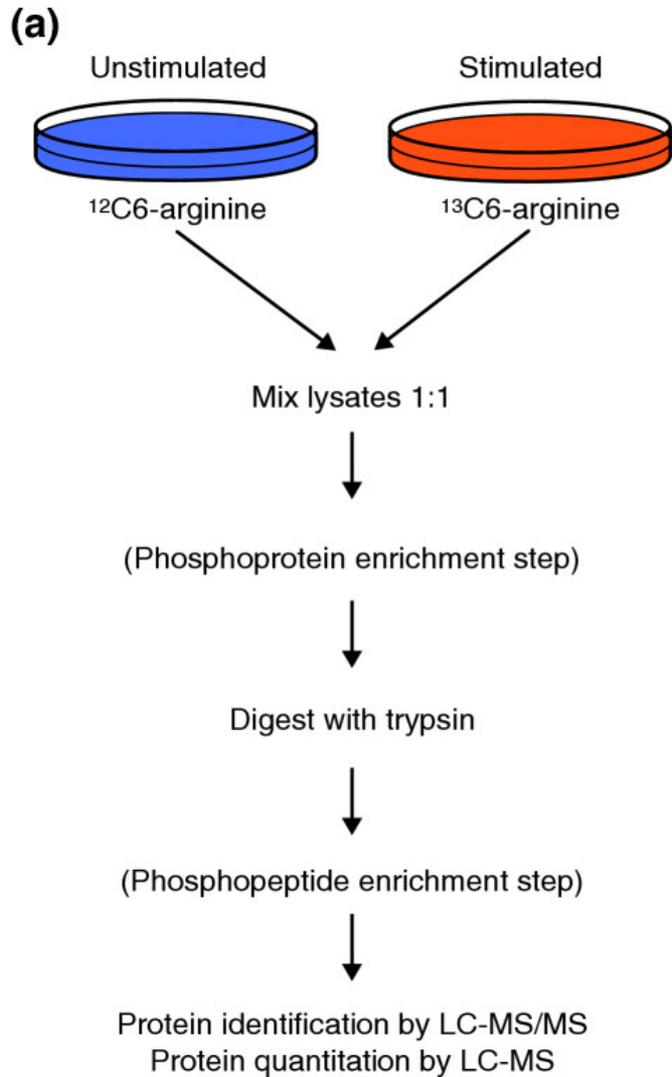
SILAC Quantification

- Experimental techniques
- MaxQuant algorithm

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SILAC



SILAC Analysis

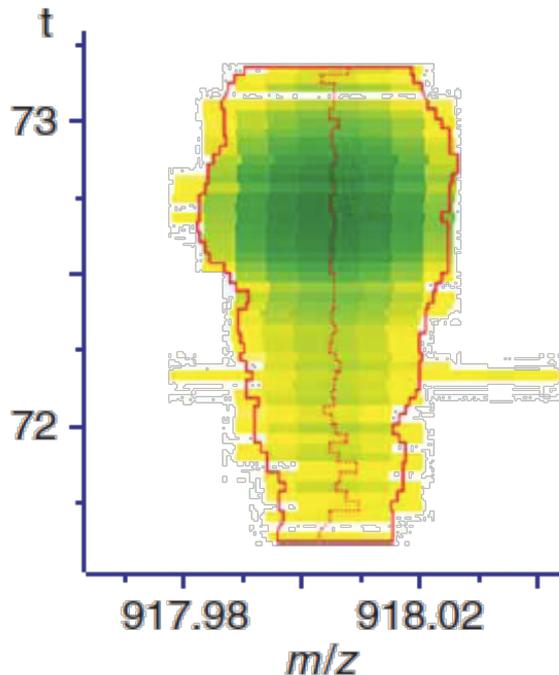
- In principle, SILAC pairs are regular features
- Note that isotopic labels shift the average model
- A standard analysis workflow could thus look like:
 - Feature finding
 - Linking of pairs with the proper distance (4/6/8/10 Da, depending on the experiment)
- Specialized SILAC analysis tools can make use of the additional information contained in pairs
 - Exact mass differences
 - Presence of a second pair can increase confidence in the detection
- Inclusion of this knowledge generally improves sensitivity of the feature/pair detection

MaxQuant

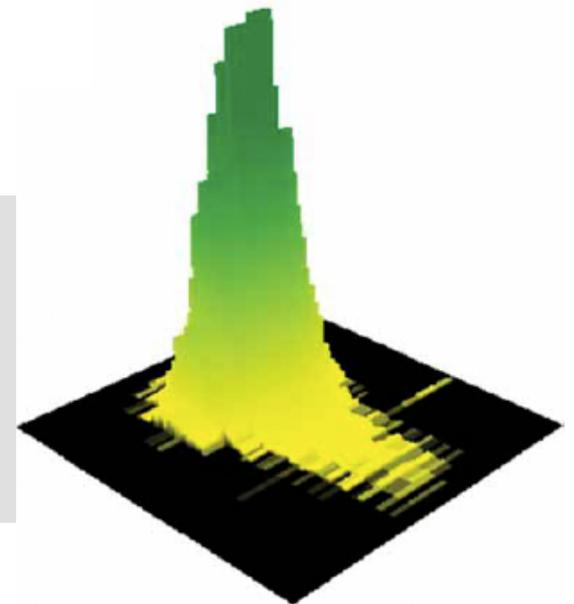
- **Peak detection**
 - Identify chromatographic peaks
- **De-Isotoping**
 - Construct features from the matching chromatographic peaks
- **Pair detection**
 - Identify SILAC pairs among the de-isotoped peaks
- **Ratio estimation**
 - Determine the ratio of the SILAC pair

Peak Detection

- MaxQuant uses the notion of **3D peaks** to describe the mass traces on the raw data (three dimensions: RT, m/z , intensity)
- 3D peaks can be defined as all the signal caused by one isotopic mass of an analyte – they correspond to mass traces in centroided feature finding
- Features are then defined as several of these 3D peaks

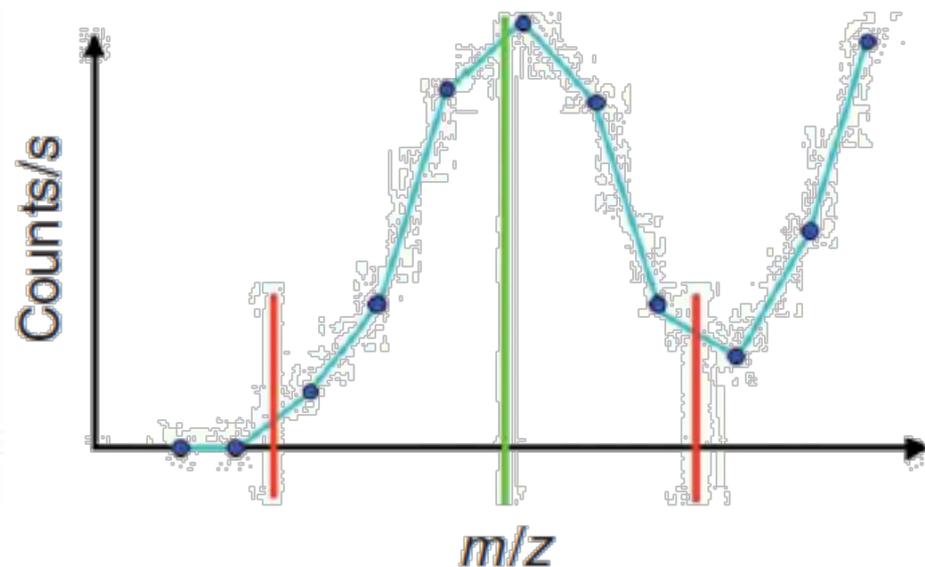
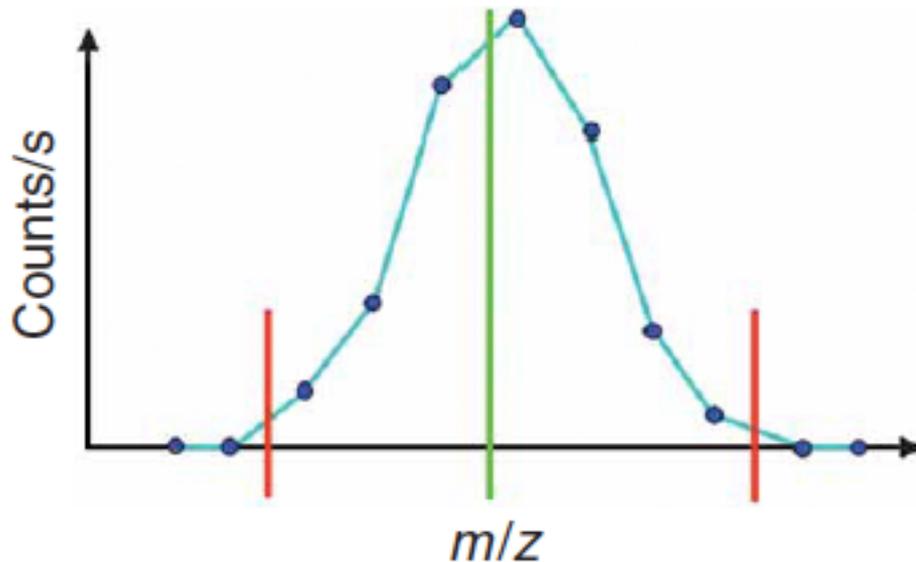


3D peak eluting over 1.5 min, m/z around 918 Da in 2D and 3D representation



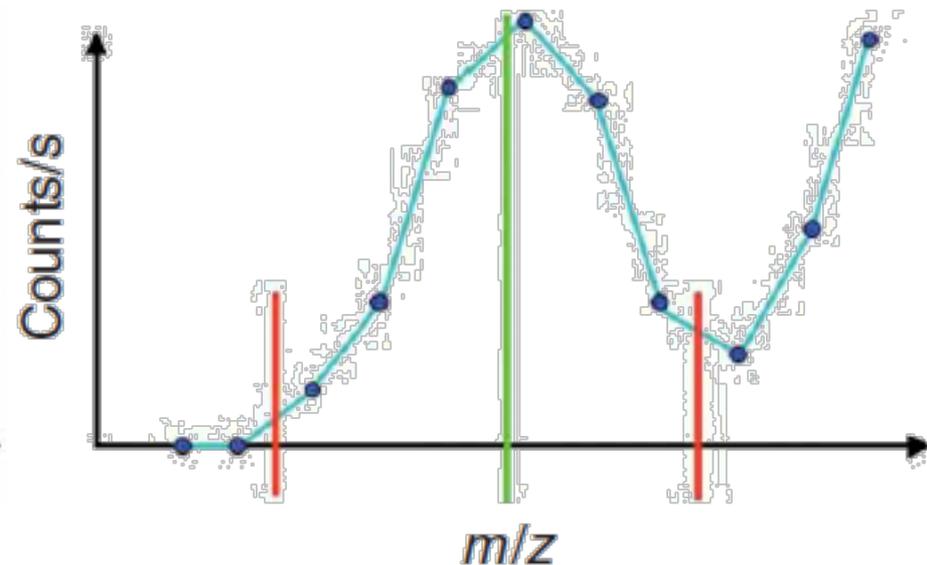
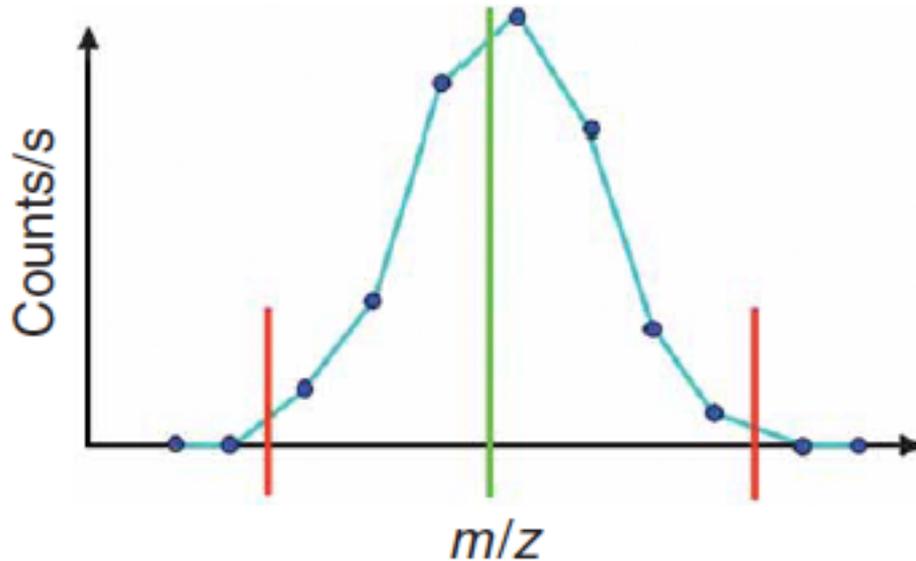
Peak Detection

- 3D peaks are detected by detecting peaks within individual mass spectra first
- For high-resolution MS instruments (e.g., Orbitrap), peak detection is achieved by looking for local maxima
- 2D peaks are then determined as the range from the maximum until either zero or a local minimum has been reached



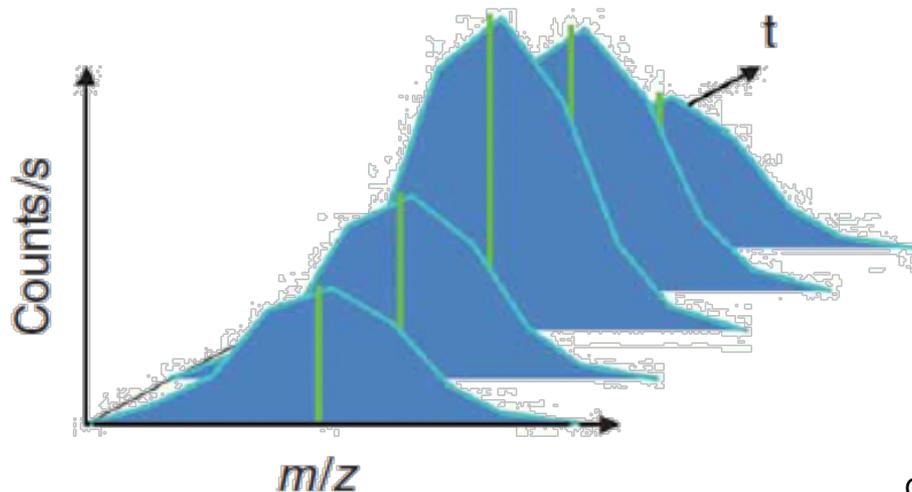
Peak Detection

- If there are more than three data points to the peak, then the center of the peak (centroid) is determined as by a **Gaussian fit** to these three peaks
- Special treatment for peaks consisting of only one or two peaks
- Intensity of the peak is approximated by the **sum of the intensities of all raw data points** of the peak



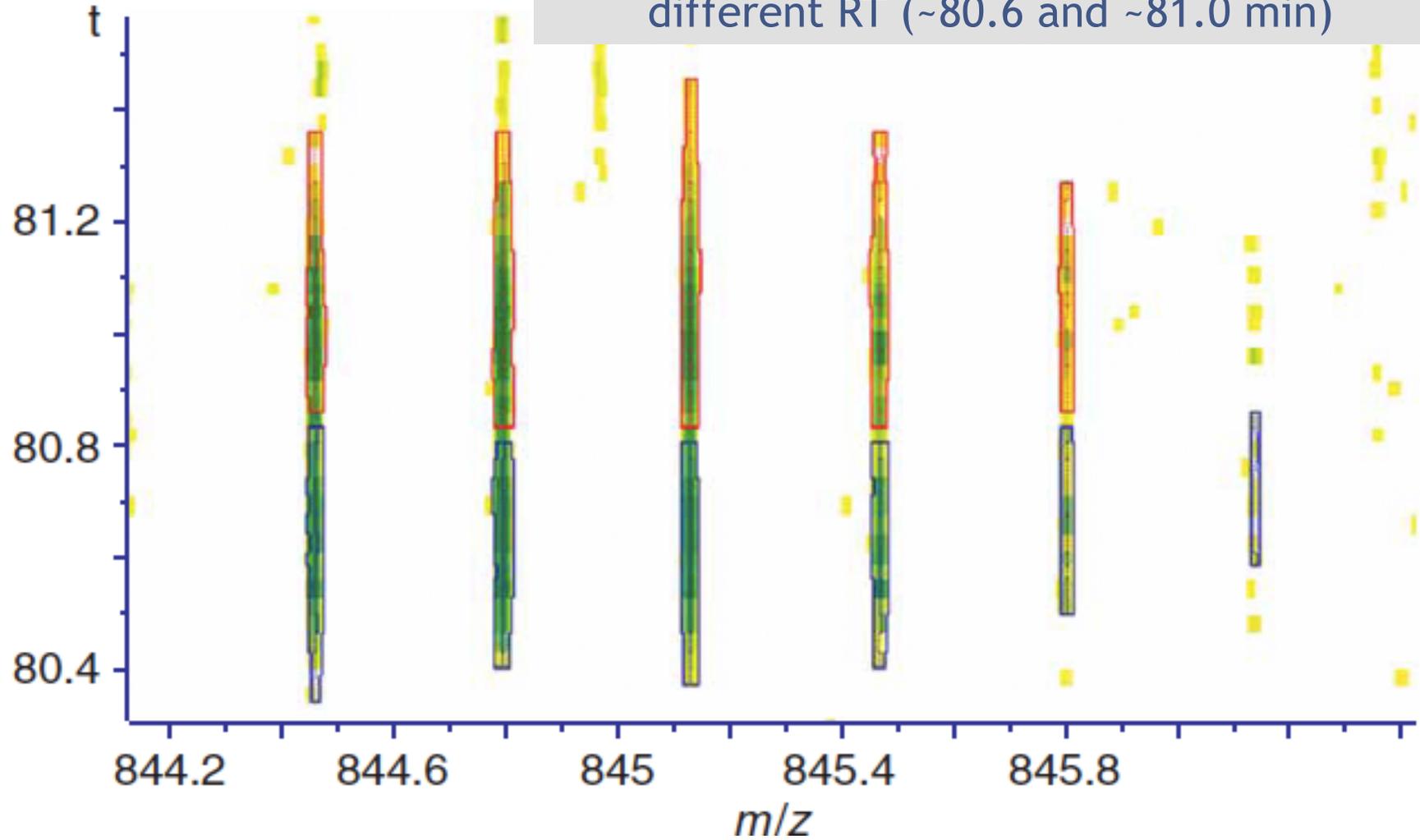
Peak Detection

- 2D peaks of adjacent scans are assembled into a 3D peak, if their centroid positions differ by less than 7 ppm
- 2D peaks may be missing in up to one scan (e.g., in case a 2D peak detection did not work well), 3D peak consists of the maximum number of 2D peaks that can be joined in this way
- Intensities of 2D peaks are smoothed and the 3D feature is split if there are local minima in the intensity
- The 3D peak mass the intensity-weighted average of its 2D peaks' masses



Peak Detection

Two 3D peaks with identical masses, but different RT (~80.6 and ~81.0 min)



De-Isotoping

- 3D peaks are aggregated to features
- To this end, a **compatibility graph** is constructed
- **3D peaks are represented by nodes**
- An **edge** is added between two nodes, if
 - Their masses match the distance within an isotope profile
 - Their elution profiles overlap (normalized inner product [cosine] of the two 3D peaks is greater than 0.6)
- **Connected components** of this graph are potential features, but can still contain 3D peaks from multiple features (overlapping features)

De-Isotoping

The mass criterion for an edge between the nodes representing two 3D peaks is fulfilled if the following holds:

$$\left| \Delta m - \frac{\Delta M}{z} \right| \leq \sqrt{\left(\frac{\Delta S}{z} \right)^2 + (5\Delta m_1)^2 + (5\Delta m_2)^2}$$

Where m is the mass difference between the peaks and ΔM is the mass difference between the monoisotopic and the ^{13}C satellite for an average of mass 1,500 Da (1.00286864 Da), z the charge.

Δm_1 and Δm_2 are the bootstrapped standard deviations of the two exact peak masses and

$$\Delta S = 2 m(^{13}\text{C}) - 2 m(^{12}\text{C}) - m(^{34}\text{S}) - m(^{32}\text{S}) = 0.0109135 \text{ Da}$$

Is the maximum mass shift caused by the incorporation of one sulphur atom.

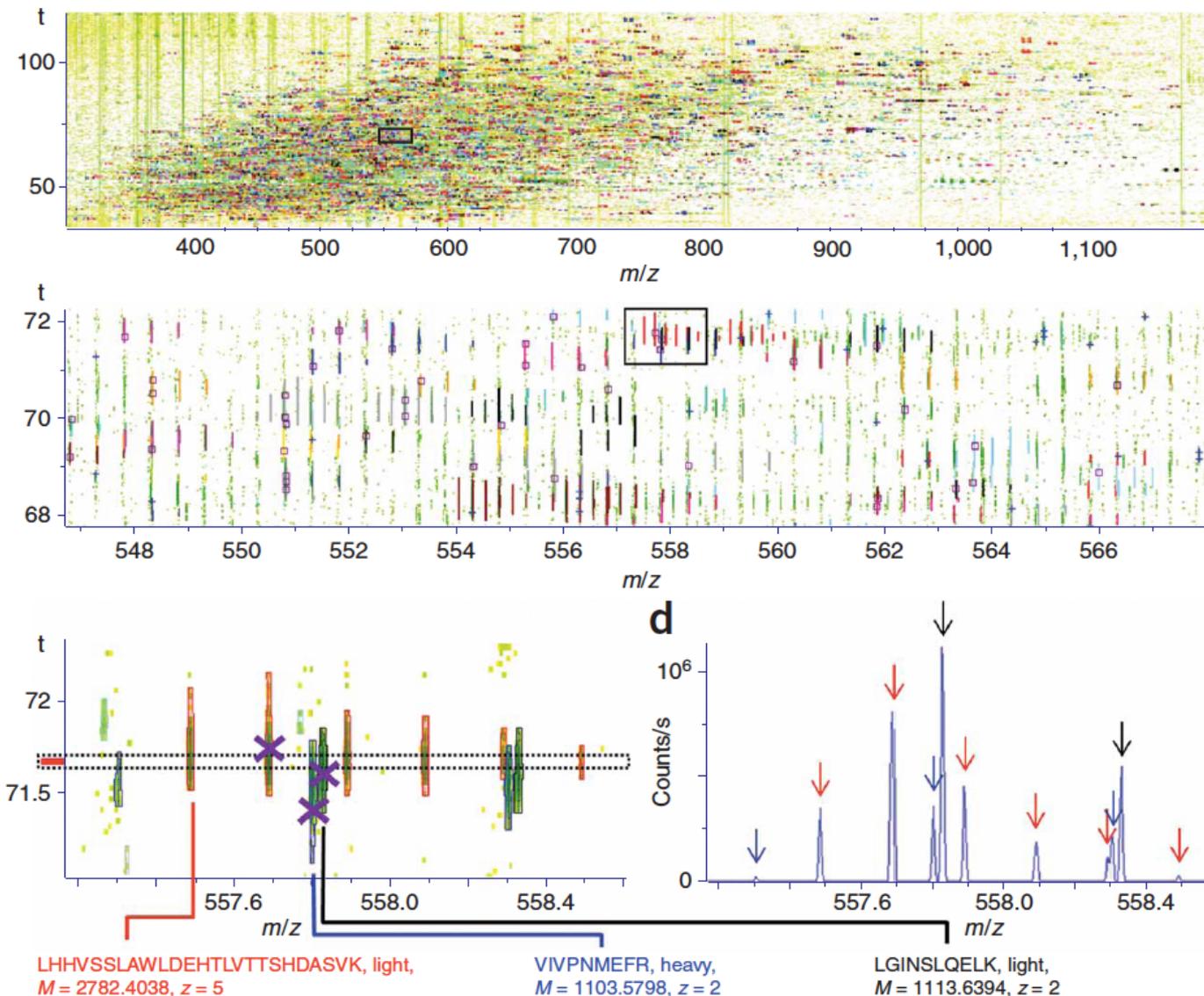
De-Isotoping

- Connected components of this graph correspond to sets of overlapping features and individual (noise) 3D peaks
- They are resolved by iteratively removing the largest set of 3D peaks that are consistent
- Consistency is defined by
 - Mutual consistency of all pairs of peaks with respect to their mass distances (similar to the above definition for an edge, but also between more distant peaks)
 - Correlation of 0.6 or better between all elution profiles
 - Correlation of 0.6 or better of the 3D peak distances with the isotope distribution of an average at mass 1,500 Da

Pair Detection and Ratio Estimation

- SILAC pairs are found through their distances by searching for pairs in the correct distance (for up to three labeled K or R in all possible combinations)
- Intensities of the two features have to have a correlation of 0.5 or better
- For each pair, the intensity ratios are determined as the slope of a regression line through the intensities of corresponding 3D peaks in the light and heavy feature

Result



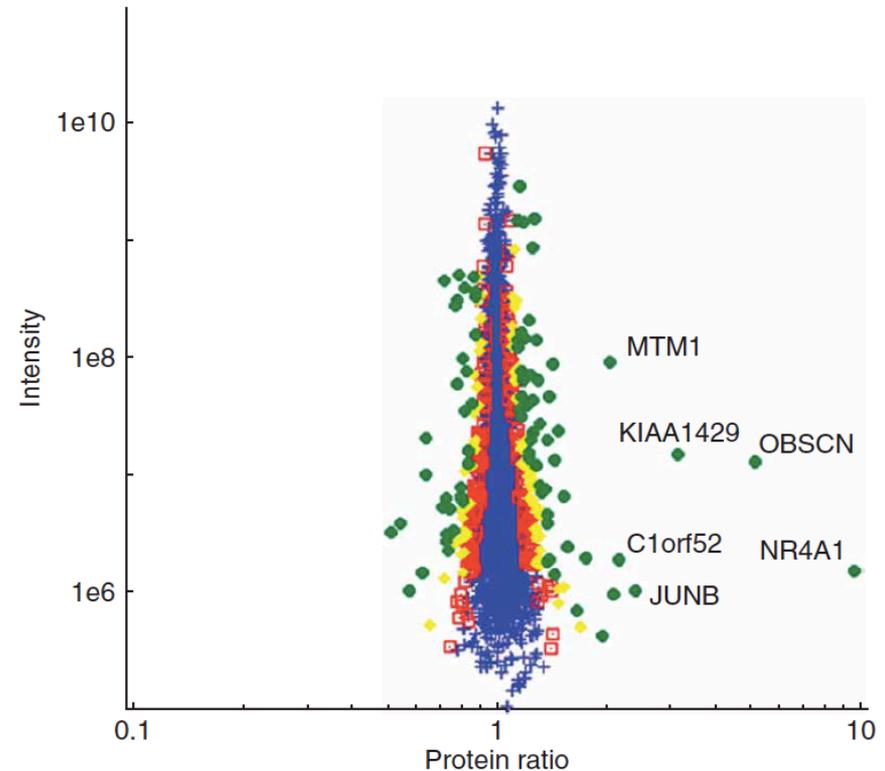
SILAC pairs identified in a large-scale study of human HeLa cells. Over 5,000 SILAC pairs were found in one run.

MaxQuant

- MaxQuant implements the SILAC pair detection algorithm sketched here
- Later versions of MaxQuant can also be applied to label-free quantification
- MaxQuant is unfortunately restricted to a specific vendor format (ThermoFischer RAW format) and platform (Windows)
- The output consists of a text file, that can then be parsed and analyzed statistically with other tools

MaxQuant

- Differential quantification of protein ratios of HeLA cells after 2 h of EGF stimulation
- 99.3% of all proteins have a ratio of 1.0 (+/- 50%) and are thus not significantly regulated
- Transcription factor JunB and orphan nuclear receptor NR4A1 are both significantly upregulated
- Their upregulation by EGF has been found through other methods and described in literature as well



'christmas tree plot':

pair intensity as a function of the pair ratio (double logarithmic plot) reveals the distribution of ratios, accuracy, LOD, LOQ, LOL

Original Papers

- Label-free feature finding (OpenMS feature finder)
 - Clemens Gröpl, Eva Lange, Knut Reinert, Oliver Kohlbacher, Marc Sturm, Christian G. Huber, Bettina M. Mayr, Christoph L. Klein: Algorithms for the Automated Absolute Quantification of Diagnostic Markers in Complex Proteomics Samples. *CompLife* 2005: 151-162.
Online: <http://www.springerlink.com/content/81lk5vjtxqwbflce/>
 - Sturm, Marc: OpenMS – A framework for computational mass spectrometry, Dissertation, Tübingen (2010)
Online: <http://nbn-resolving.de/urn:nbn:de:bsz:21-opus-51146>
 - Website: <http://openms.de>
- SILAC feature finding (MaxQuant)
 - Cox, J. and Mann, M. (2008) MaxQuant enables high peptide identification rates, individualized p.p.b.-range mass accuracies and proteome-wide protein quantification. *Nat Biotechnol* 26, 1367-72.
(algorithm: see Supplementary Material at <http://www.nature.com/nbt/journal/v26/n12/extref/nbt.1511-S1.pdf>)
 - Website: <http://maxquant.org>

Materials

- Online Materials
 - Learning Unit 5[A,B,C],
 - Learning Unit 1C